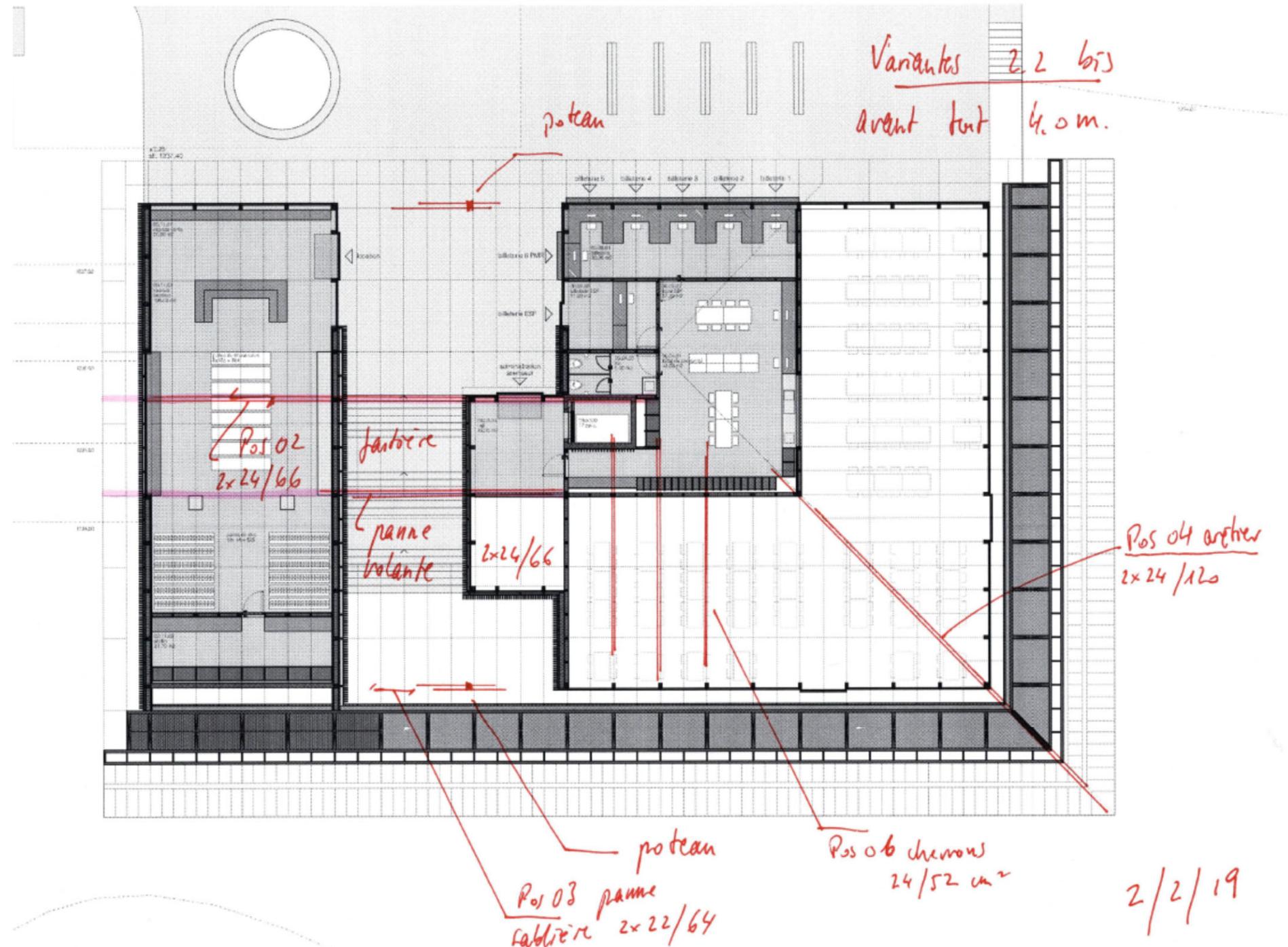


# Beam and cantliver systems

Natterer Johannes

Ing. dipl. EPFL

EPFL - SGC



**Comparatif des coûts**

		non structure	structure	total					
Variantes		Prix SNP +/- 20% CHF	Prix SP +/- 20% CHF	Prix total +/- 20% CHF	Av. toit 5,5m	Av. toit 4,0m	entraxe chevrons Pos.06 = 2,0m	entraxe chevrons Pos.06 = 0,6m	Appui supplémentaire sablière Pos.03
Caisson		340 172	622 009	962 181	x				
chevron	1.1	354 442	432 657	787 099	x		x		
	1.2	354 442	423 326	777 768	x		x		x
	2.1	337 690	359 157	696 847		x	x		
	2.2	337 690	338 882	676 572		x	x		x
	2.2.bis	337 690	315 671	653 361		x	x		x
	3.1	354 442	616 937	971 379	x			x	
	3.2	354 442	597 929	952 371	x			x	x
	4.1	354 442	465 675	820 117		x		x	
	4.2	354 442	447 704	802 146		x		x	x

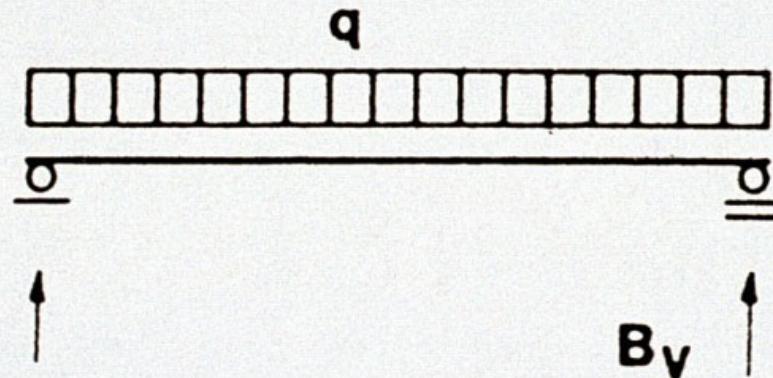
# Konrad Merz, kley und partner





# The beam on 2 supports with uniform charged loads

Poutres sur deux appuis,  
ouvrages porteurs



charges:  
charges uniformément réparties,  
verticales

# Solid wood

# Solid wood

## ■ Limit of the section

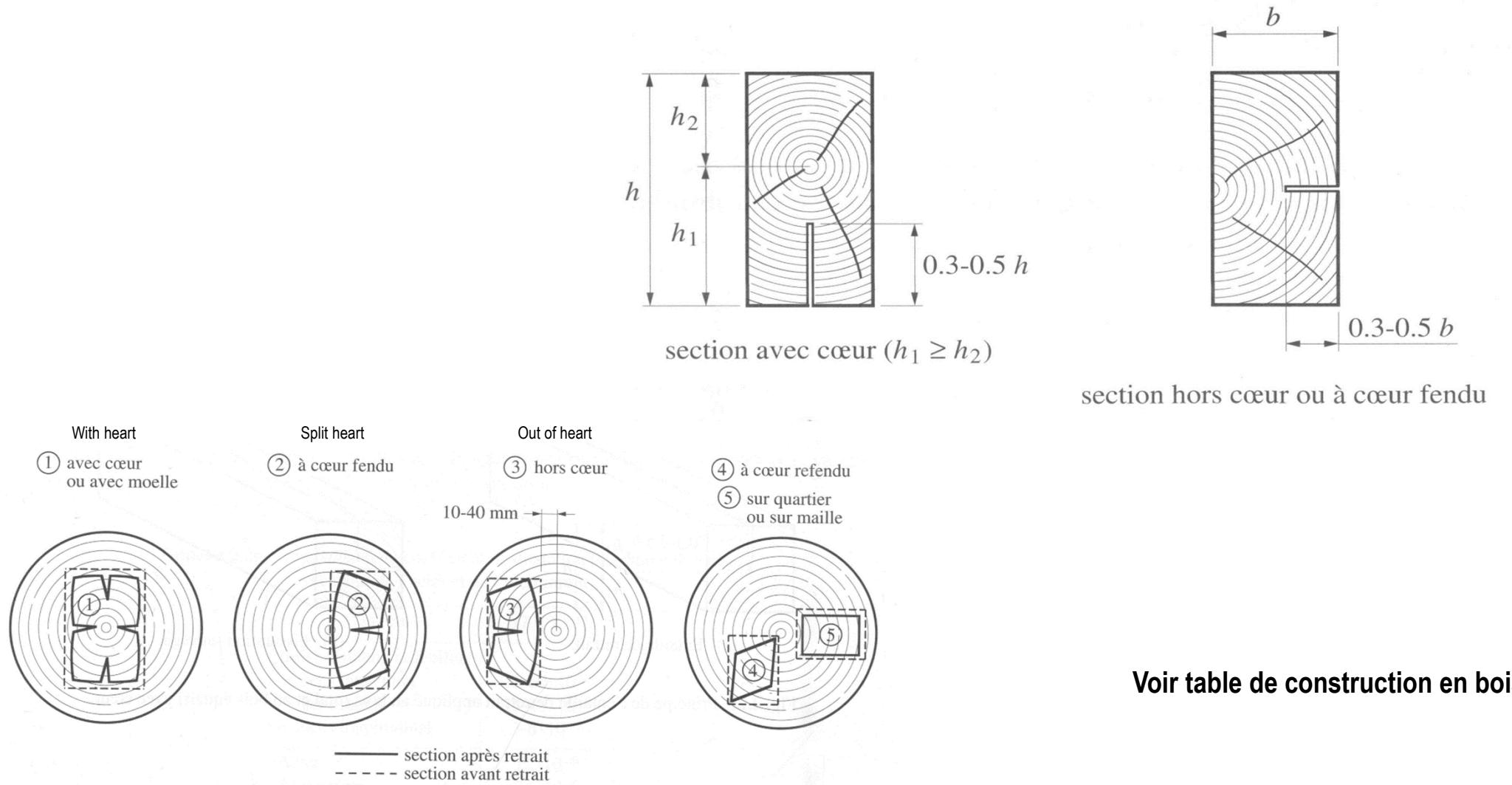


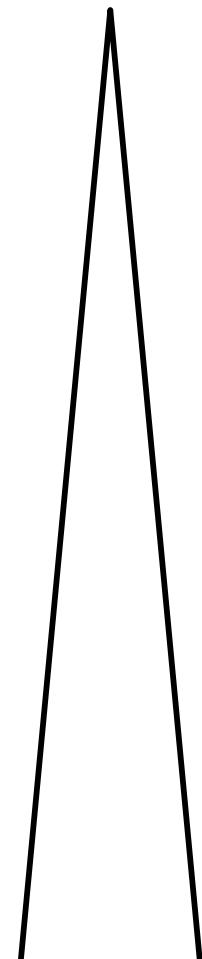
Fig. 2.24 Déformations et fissurations des sections pour les principaux modes de débit.

# The origin of wood

- The trunk of the tree

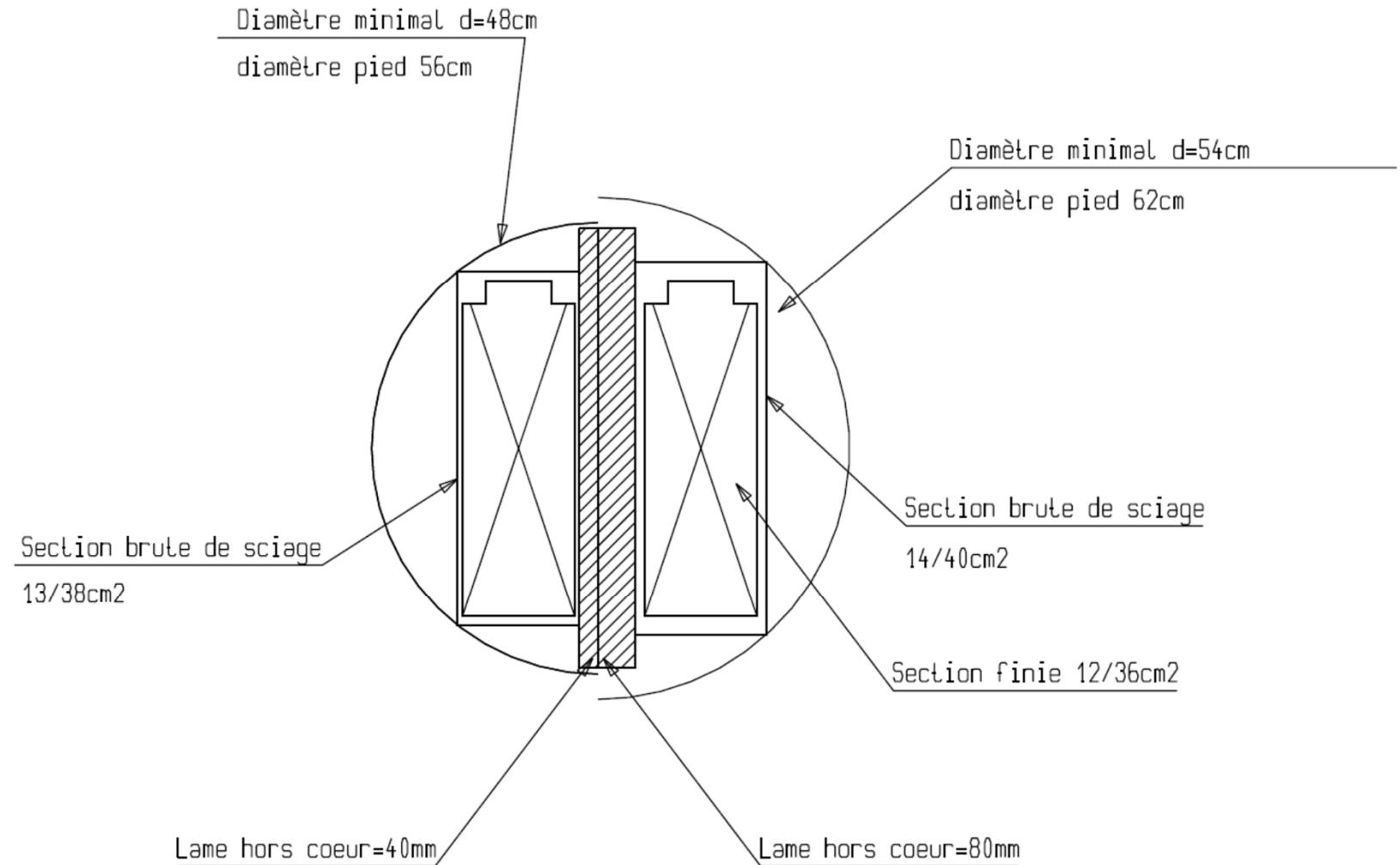


The shaft of the tree  
about 1cm/meter



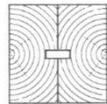
# Solid wood beam

## ■ Project of Ursy

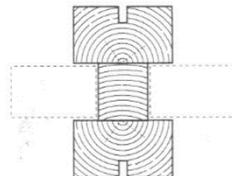


# Composed sections

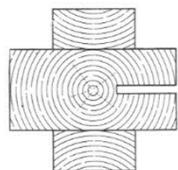
- To increase the surface – inertia -> the resistance



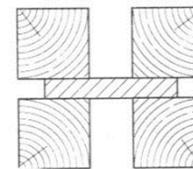
à partir de madriers à cœur refendu,  
avec gorge de décharge à l'intérieur



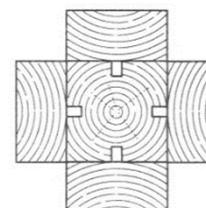
profil en I à partir de madriers



section en croix à partir de trois madriers

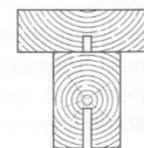


section rectangulaire composée d'un  
bastaing et de quatre madriers



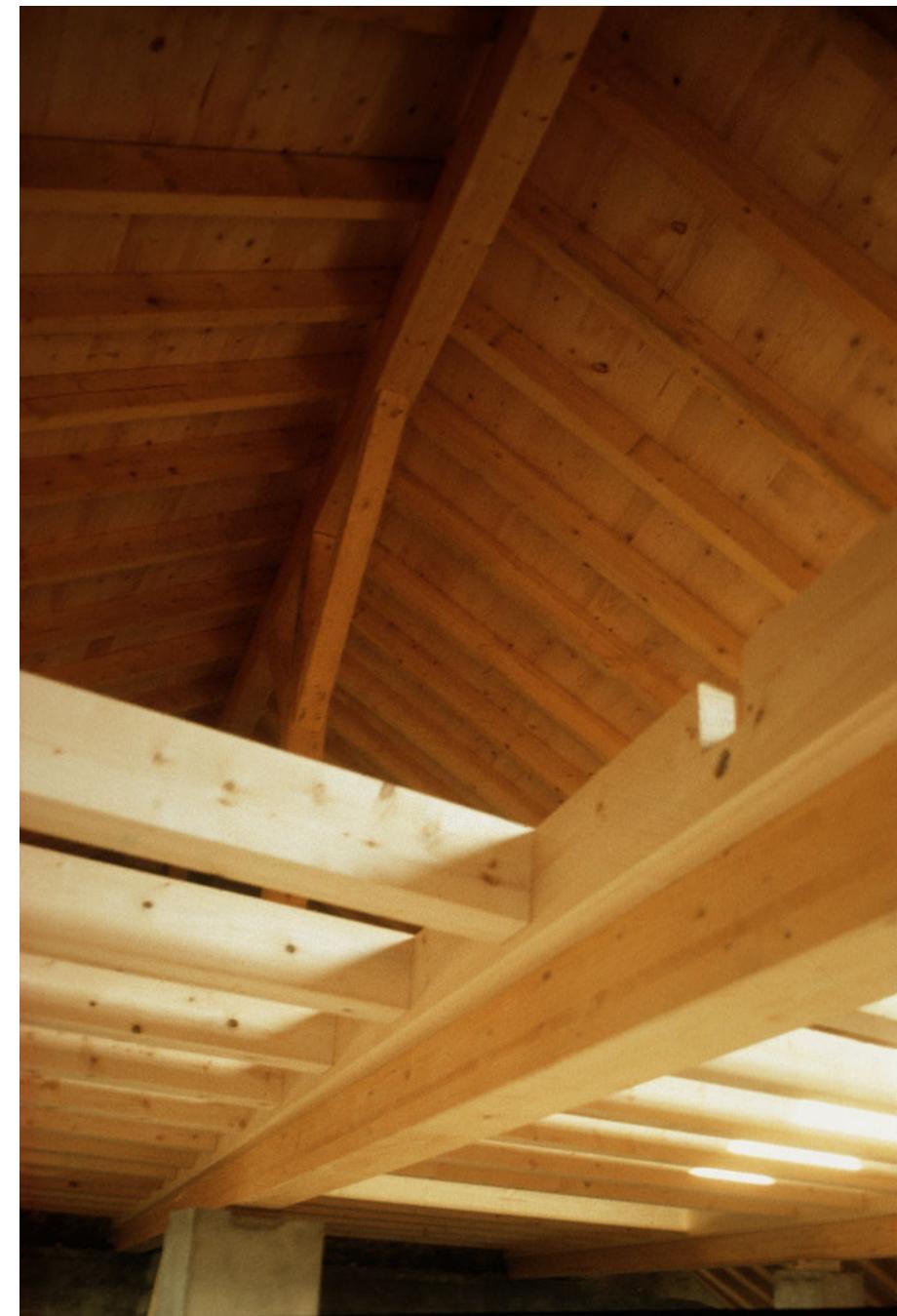
section en croix avec madrier et quatre  
bastaings

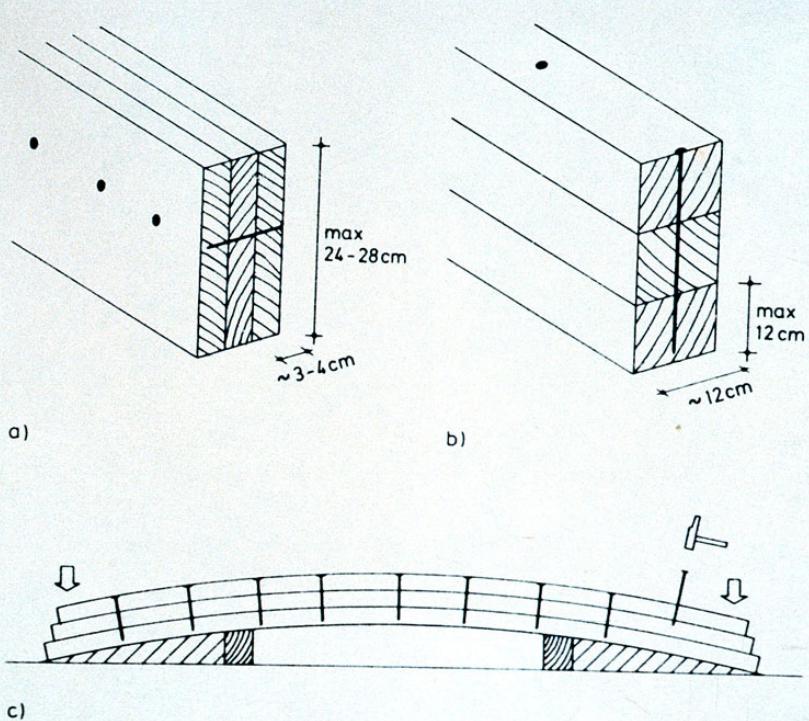
Sections composées de poutres







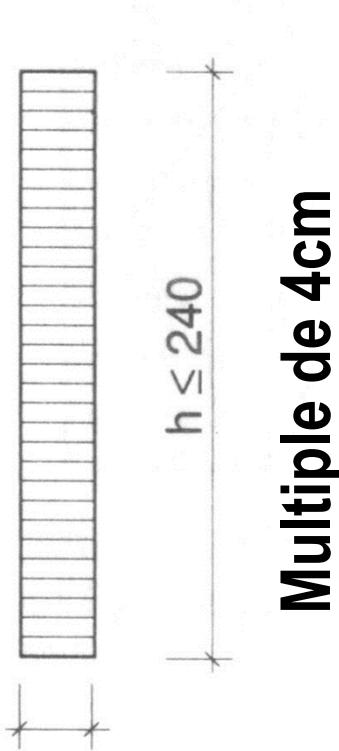






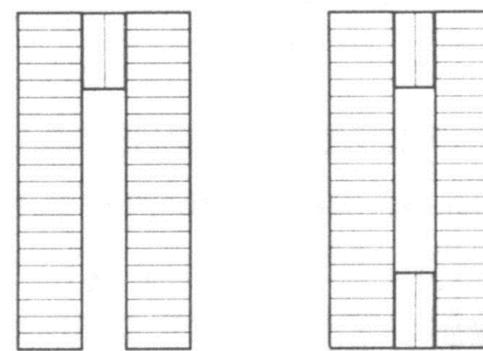
# Glue laminated beams

# Limit section



**Multiple de 4cm**

**$12 < b < 24 \text{ cm}$**

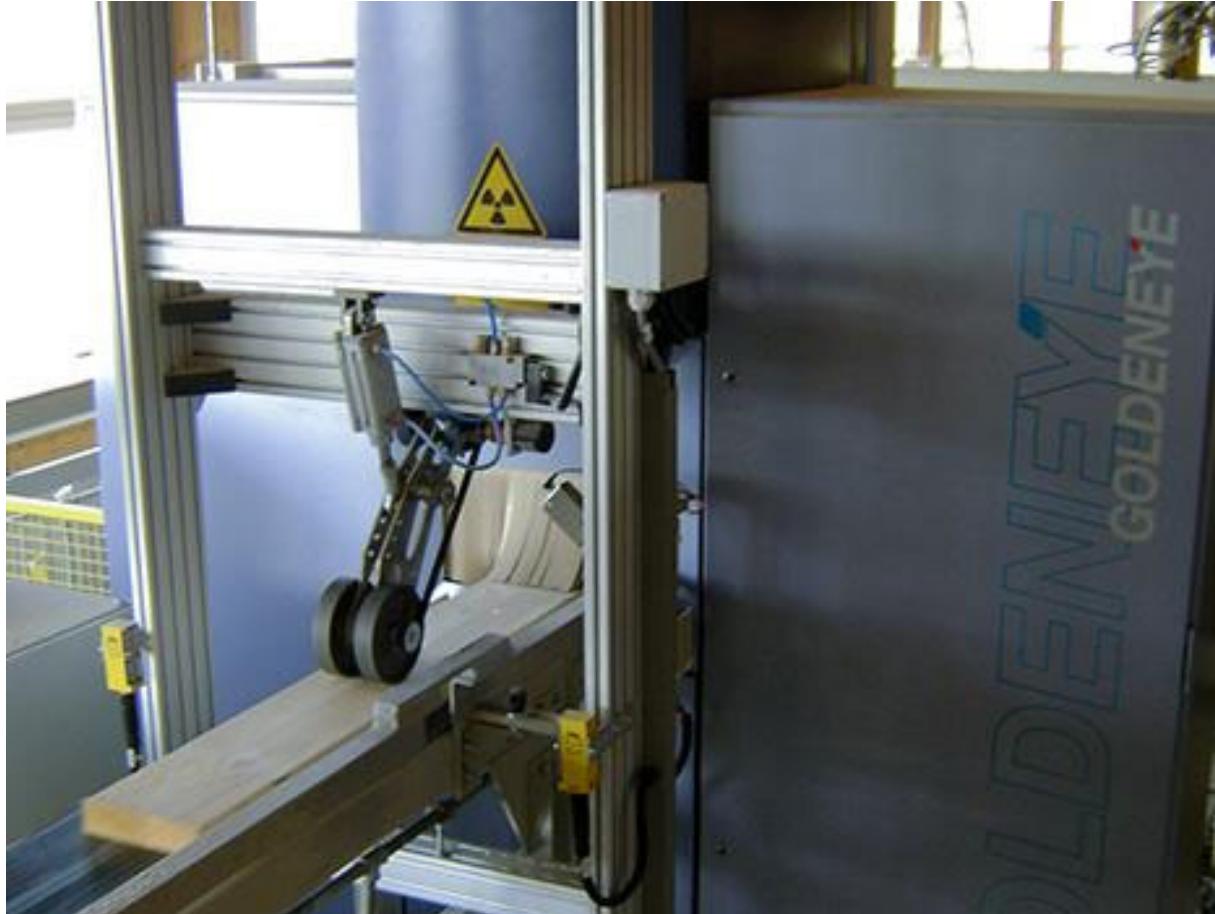


section en U retourné, section à caisson

# The manufacturing

- Sawing into boards Drying -> 12%
- Sorting
- Jointing
- Gluing
- Clamping and drying
- Size and finishing

# Sorting – Golden Eye



Some points:

Sorting speed: up to 450m/minute

Measurement:

average wood density  
humidity/moisture  
rate of knot density

# Classification of boards for GlueLam

## Propriétés des lames

Les lames et leurs joints longitudinaux (en règle générale des aboutages dentelés) doivent correspondre aux caractéristiques du tableau 11 (EN 1194):

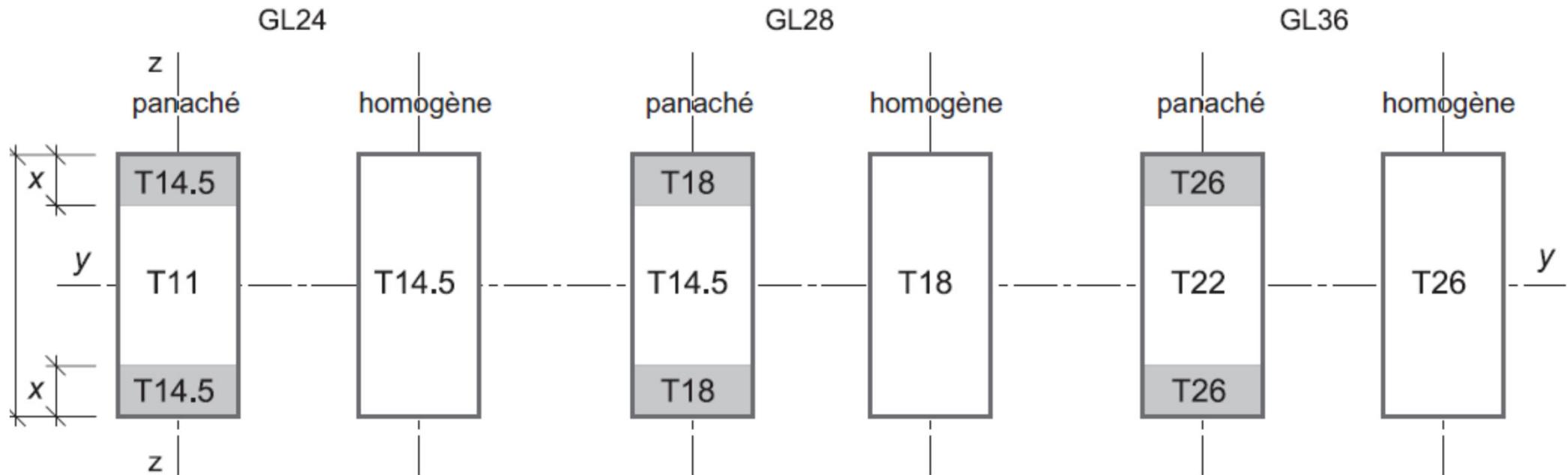
Tableau 11: Exigences relatives aux propriétés des lames et des aboutages

Désignation des lames	T11	T14.5	T18	T22 <sup>3)</sup>	T26 <sup>3)</sup>
Valeur caractéristique de la résistance à la traction, en N/mm <sup>2</sup> $f_{t,0,l,k}$ <sup>1)</sup>	11	14,5	18	22	26
Module E moyen en traction, en kN/mm <sup>2</sup> $E_{t,0,mean}$	9	11	12	13	14
Valeur caractéristique de la résistance à la traction des aboutages dentelés, en N/mm <sup>2</sup> $f_{t,j,k}$ <sup>2)</sup>	16	20	23	27	31

<sup>1)</sup> définie pour la section totale de la planche, pour une longueur libre de 2000 mm  
<sup>2)</sup> définie pour la section totale de l'aboutage, pour une longueur libre  $\geq 200$  mm  
<sup>3)</sup> vérifier les possibilités de fabrication (nécessite un tri mécanique)

# Composition of Gluelam

Figure 13: Constitution de la section de bois lamellé collé



$$x \geq \frac{h}{6}, \text{ au minimum 2 lames}$$

T11: désignation des lames

T = tension (traction)

11 = valeur caractéristique de la résistance à la traction, en N/mm<sup>2</sup>.

# Butting



# Board gluing

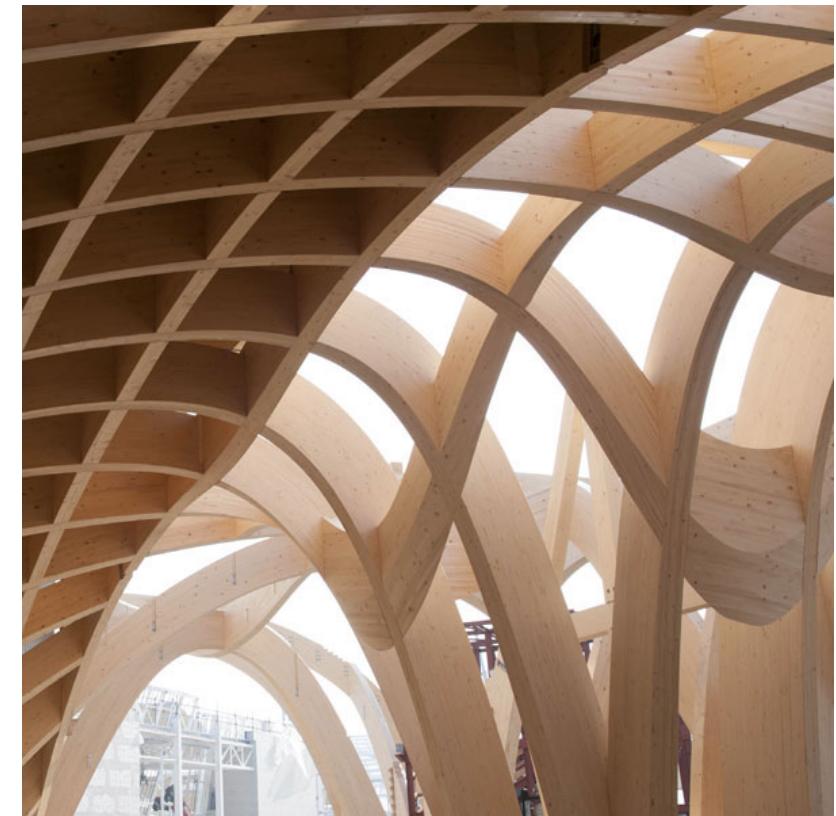


**DPF-DUCRET**

# Machining and assembly

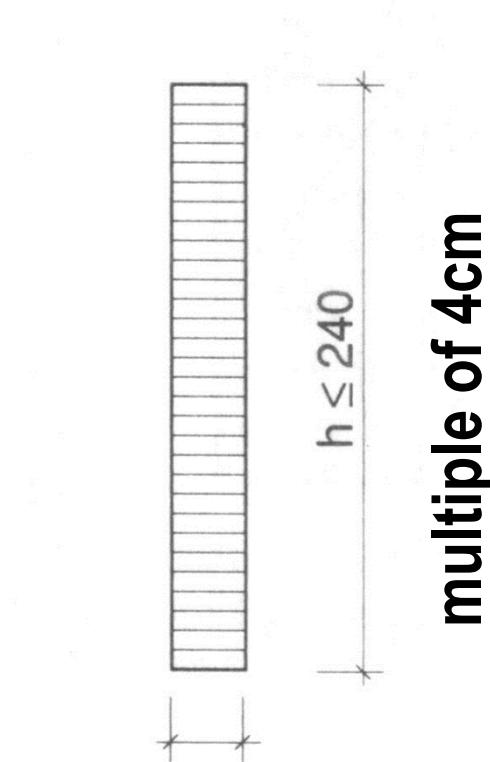


**JPF-DUCRET**



Technowood.ch

# Limit of the sections



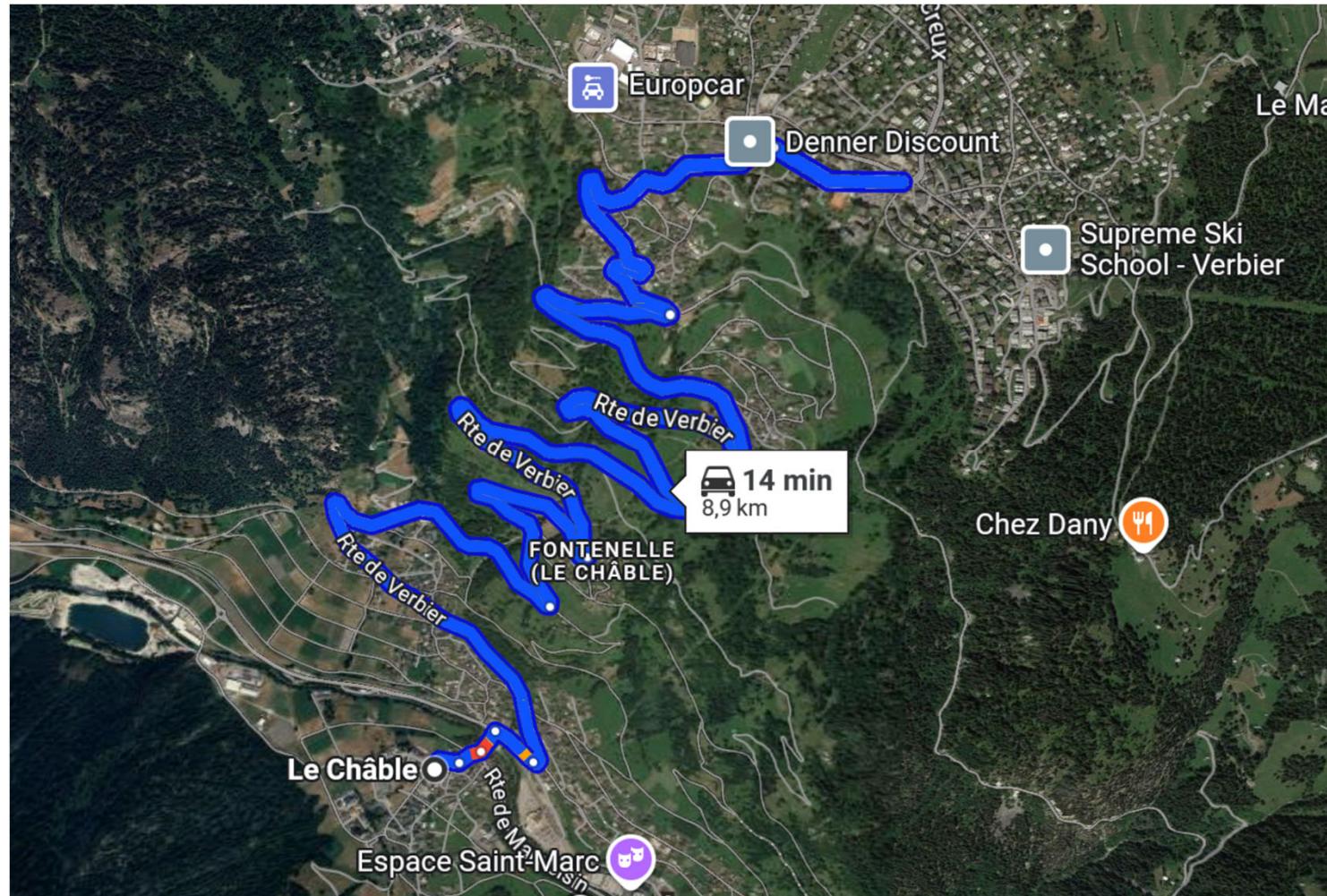
$12 \text{ cm} < b < 24 \text{ cm}$

Limit length

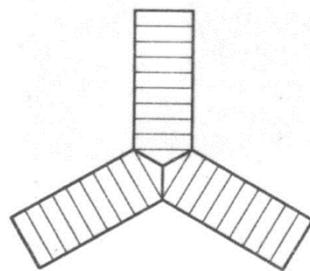
25 m - 38 m

# Limit length

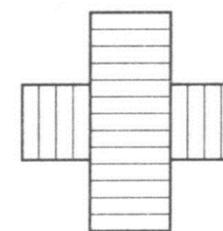
- Take care about the transport



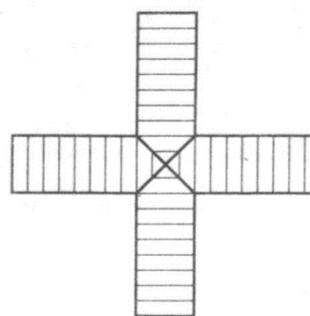
# Composed sections



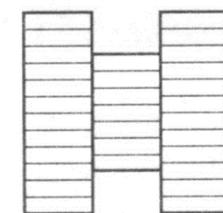
poteau triangulaire non massif



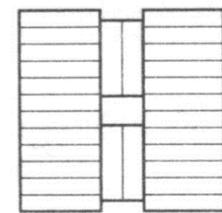
à éléments croisés

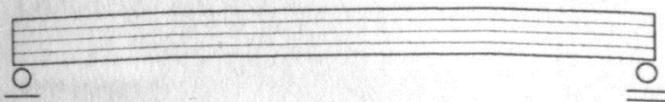


poteau en croix

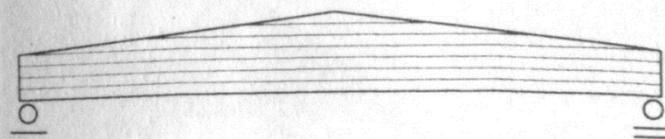


profils en I

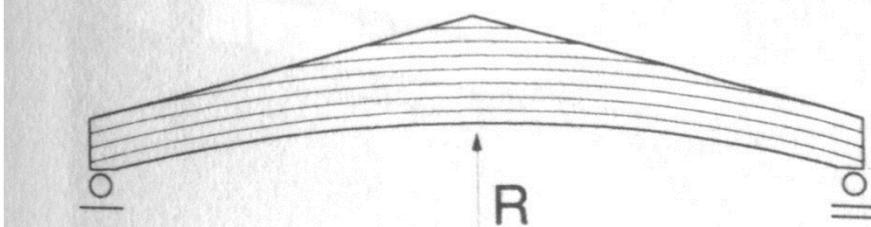




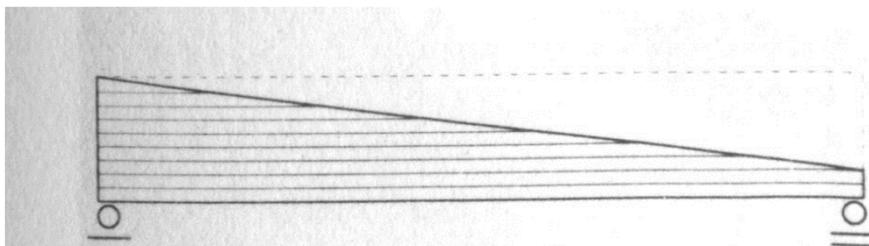
poutre lamellée-collée avec contre-flèche



poutre de toit à deux pans



poutre de toit à deux pans, incurvée



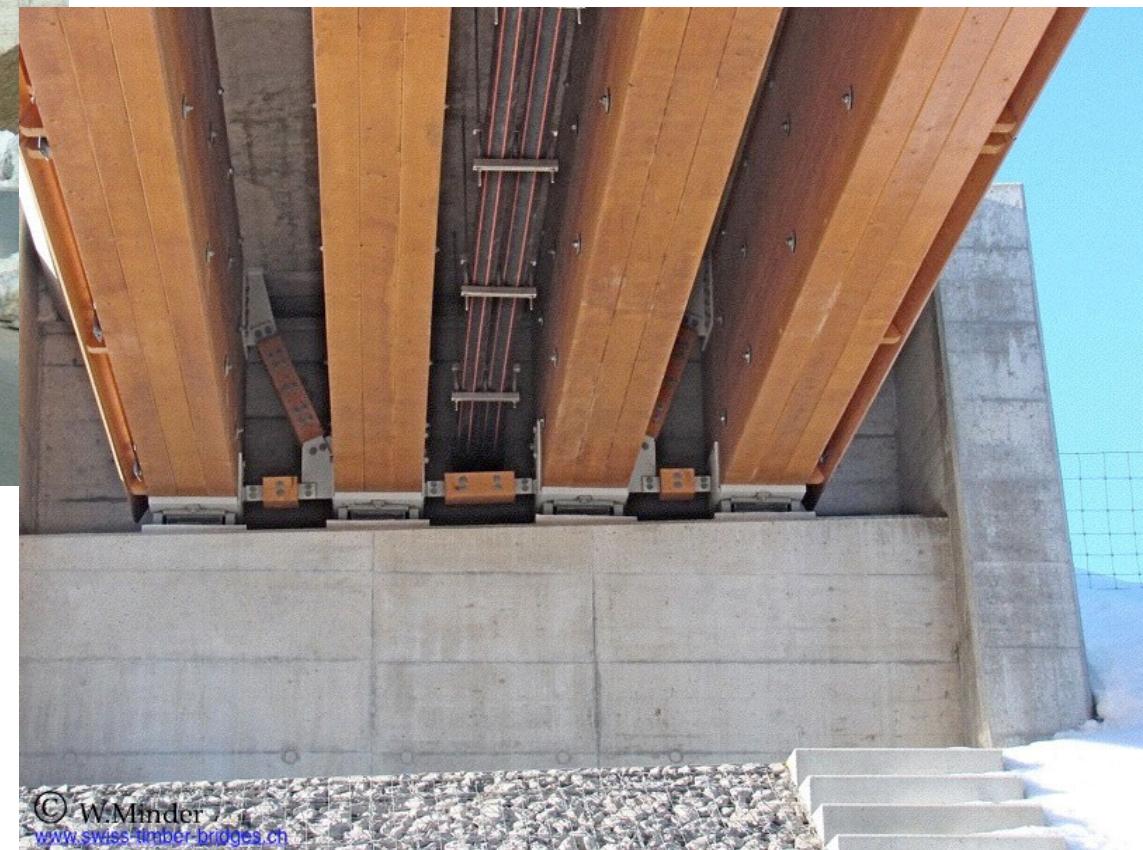
poutre rectangulaire donnant deux éléments de pan de toit





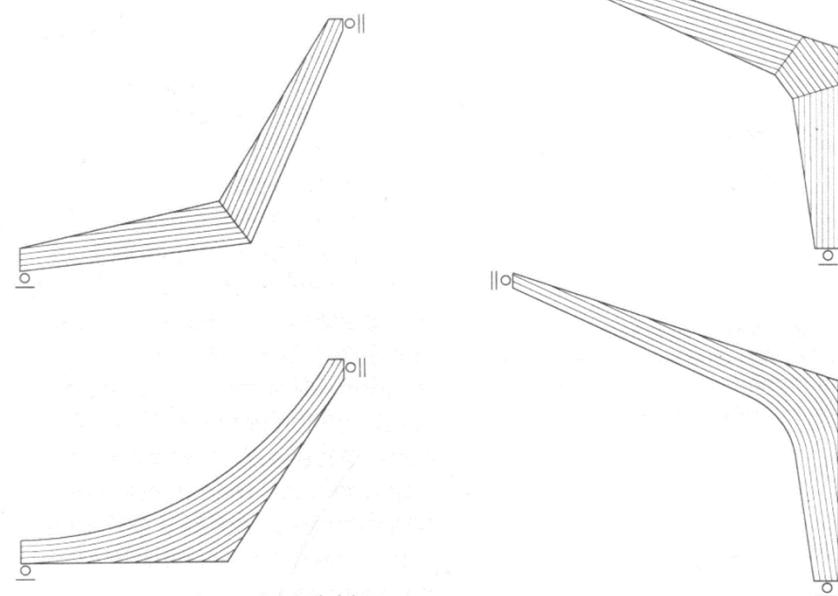


# Multi-glued laminated timber

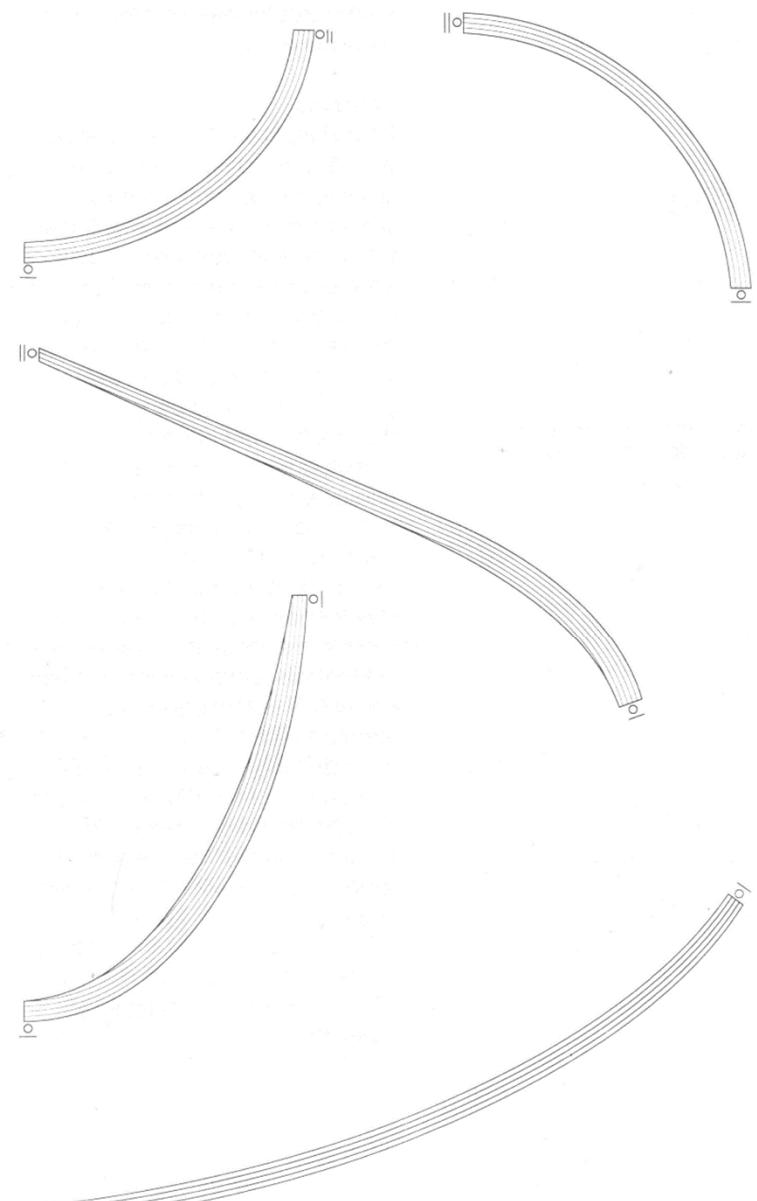




# Curved Glulam



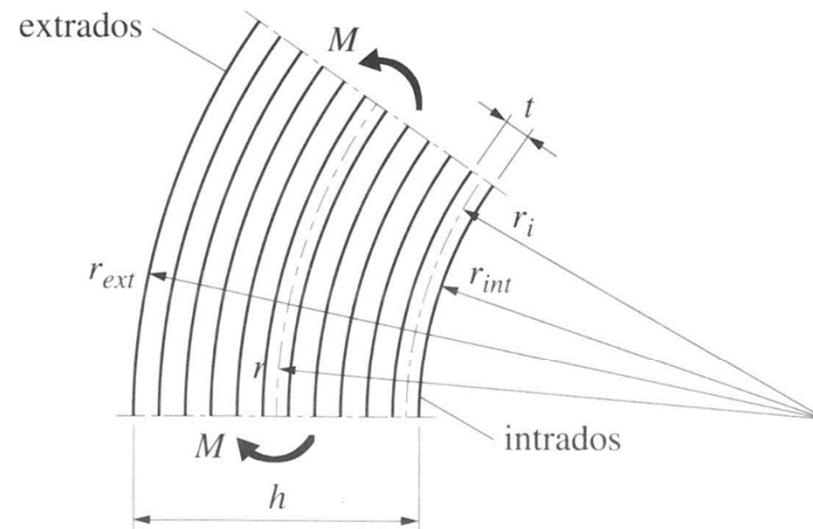
poutres à angles de portique rigides



poutres à courbure simple

# The curved

- Radius representation – inne constraint



**Fig. 6.41** Représentation des différents rayons de courbure à considérer.

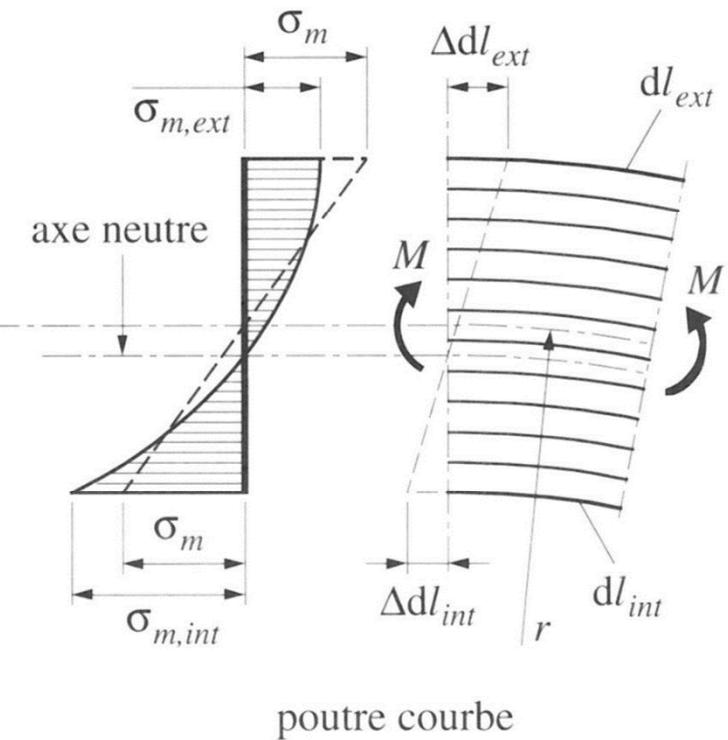
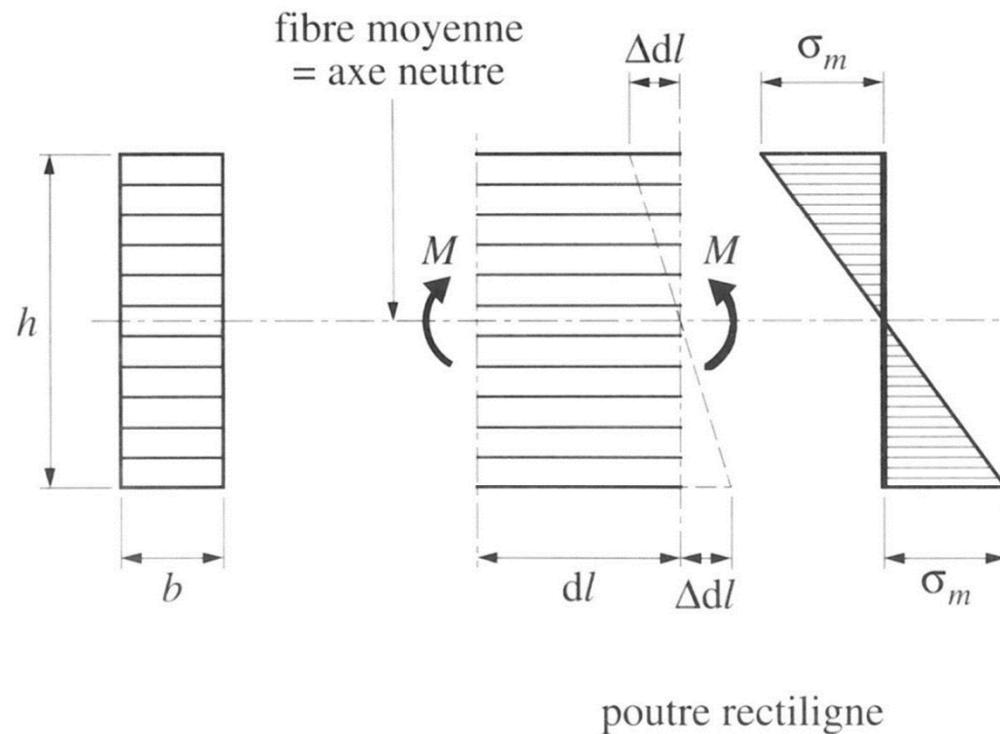
# Curved beam

- Inner constraint

$$\sigma = \frac{1}{2} \frac{E t}{r_{int}} = \frac{1}{2} \frac{10\,000 \text{ N/mm}^2}{200} = 25 \text{ N/mm}^2$$

# Curved beam

- Representation of the flexion



# Curved beam

## ■ Factor $k_{\parallel}$

$$\sigma_{m,d} = k_{\parallel} \frac{M_d}{W} \quad (6.41)$$

$\sigma_{m,d}$  : valeur de calcul de la contrainte de flexion

$k_{\parallel}$  : coefficient tenant compte de la distribution hyperbolique des contraintes de flexion pour les poutres courbes à inertie constante

$M_d$  : valeur de calcul du moment de flexion

## ■ According to eurocode 5

$$k_{\parallel} = 1 + 0.35 \left( \frac{h}{r} \right) + 0.6 \left( \frac{h}{r} \right)^2$$

## ■ Selon SIA 164

$$k_{\parallel} = 1 + \frac{h}{2r}$$

# Curved beam

- According to SIA 265

Contraintes tangentielles (parallèles au fil):

- extrados:

$$\sigma_{ma,d} = \left| -\frac{M_{Ed}}{W} \right| \leq k_r f_{m,d}$$

- intrados:

$$\sigma_{mi,d} = \left| +\frac{M_{Ed}}{W} \left( 1 + \frac{h}{2r} \right) \right| \leq f_{m,d}$$

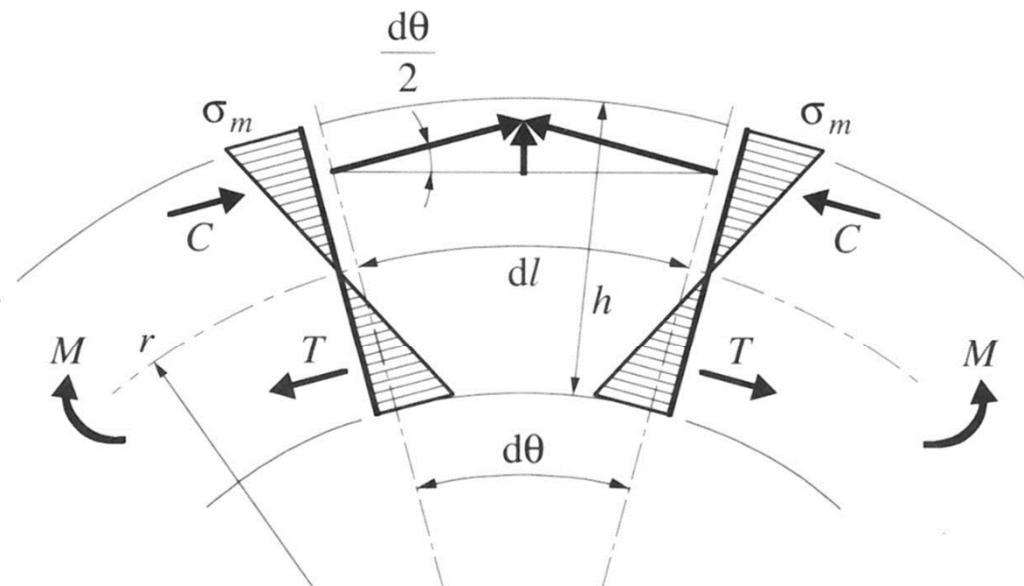
$$k_r = 1 - 40 \frac{t}{r_a}$$

$t$  épaisseur des lames

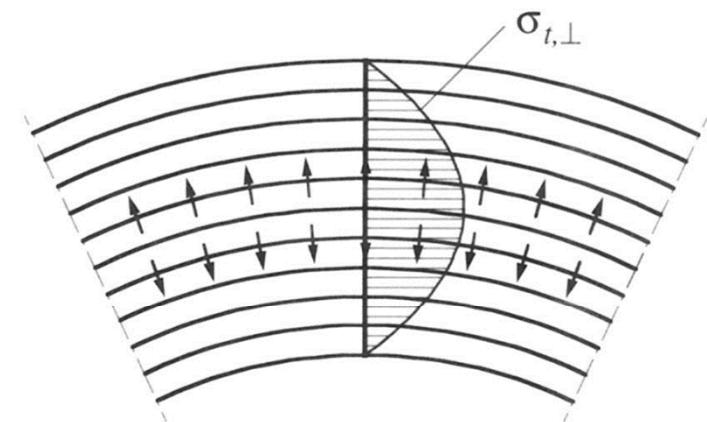
$r_a$  rayon de courbure de l'extrados.

# Curved beam

- Another special feature – traction perpendicular to the fiber



mise en évidence de la composante transversale



contrainte transversale

# Curved beam

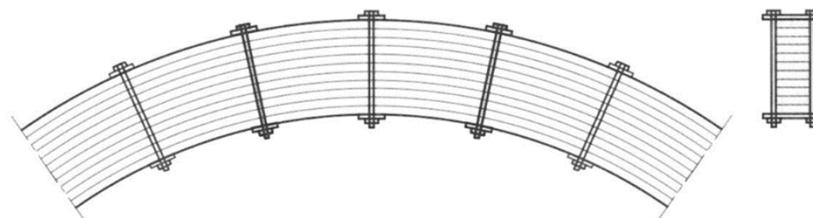
## ■ Traction perpendicular to the beam

$$\sigma_{t,\perp,d} = k_{\perp} \frac{M_d}{W} \quad (6.46)$$

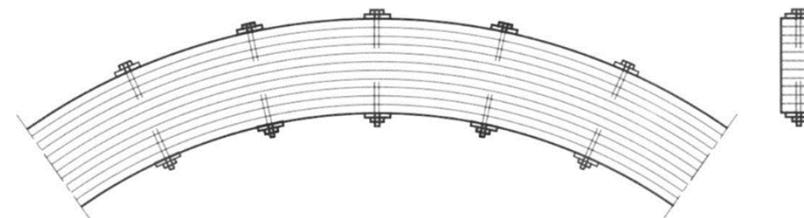
- $\sigma_{t,\perp,d}$  : valeur de calcul de la contrainte de traction perpendiculaire aux fibres
- $k_{\perp}$  : coefficient lié à la géométrie de la poutre ( $k_{\perp} = h/(4 r)$  pour une poutre courbe d'inertie constante)
- $M_d$  : valeur de calcul du moment de flexion
- $W$  : module de flexion de la section

# Curved beam

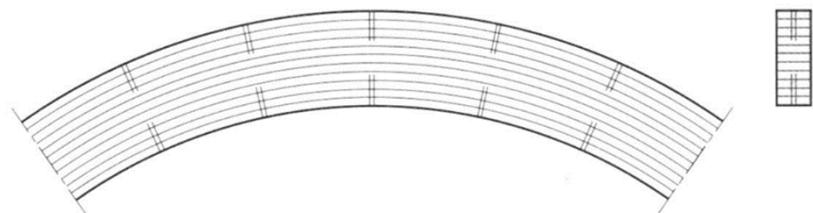
- Reinforcement perpendicular to the beam



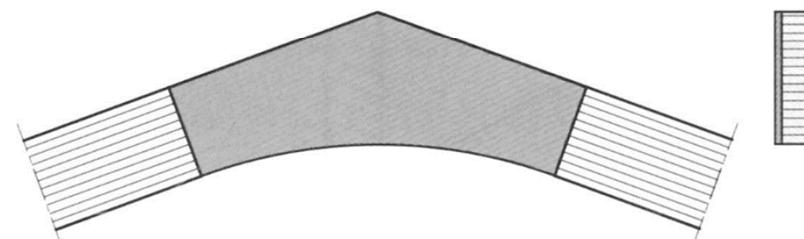
plaques et tiges filetées de chaque côté



plaques et tiges filetées à travers l'élément



tiges filetées encollées



contreplaqué de chaque côté ou fibre de verre collée

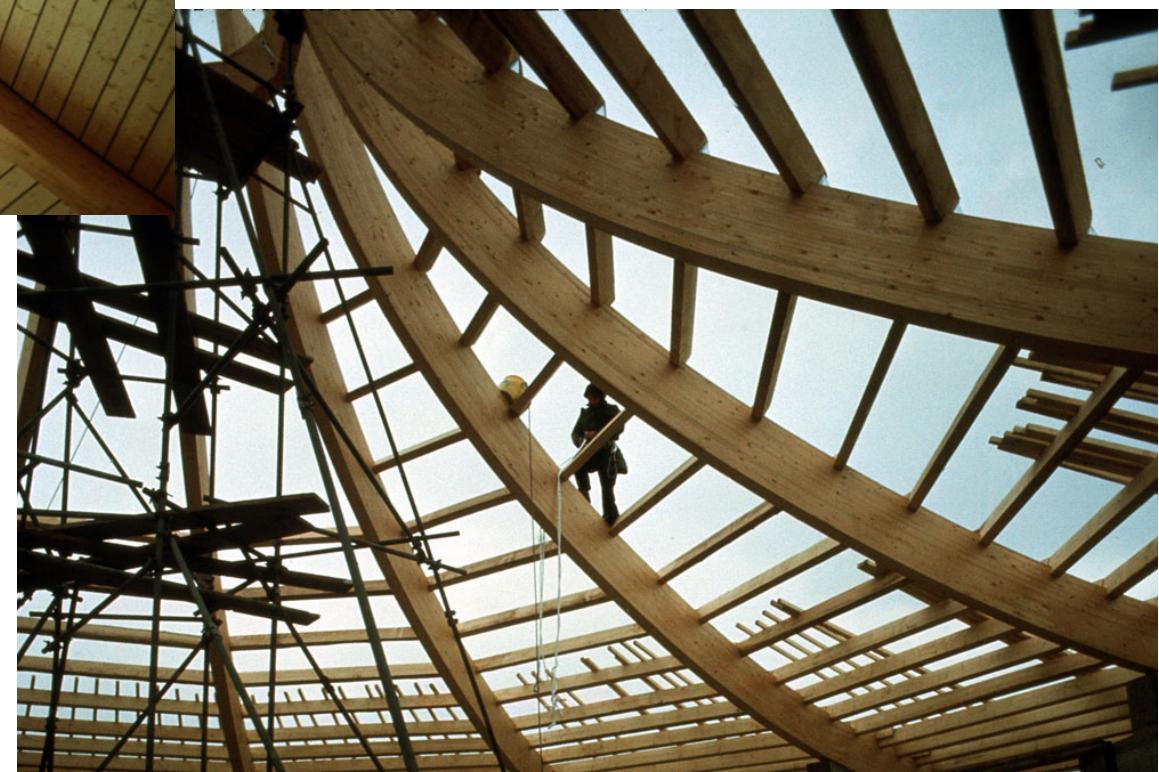
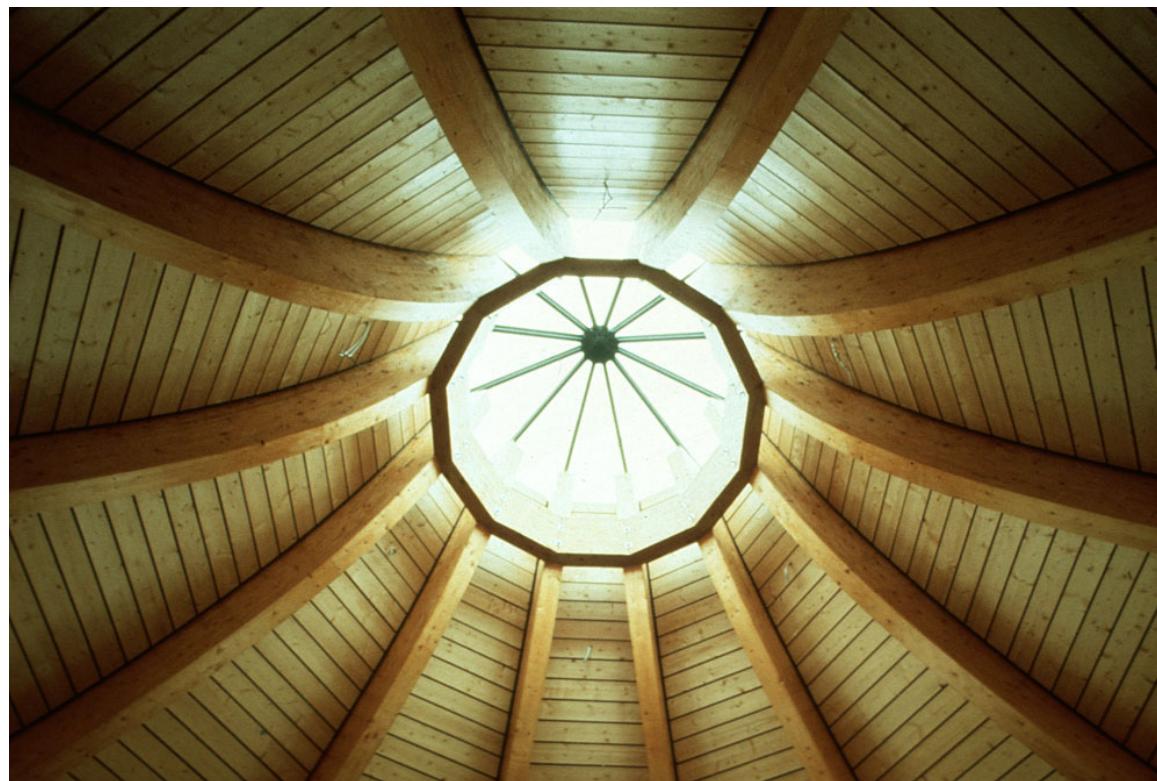
**Fig. 6.44** Systèmes de renforcements en traction perpendiculaire des arcs cintrés en bois.





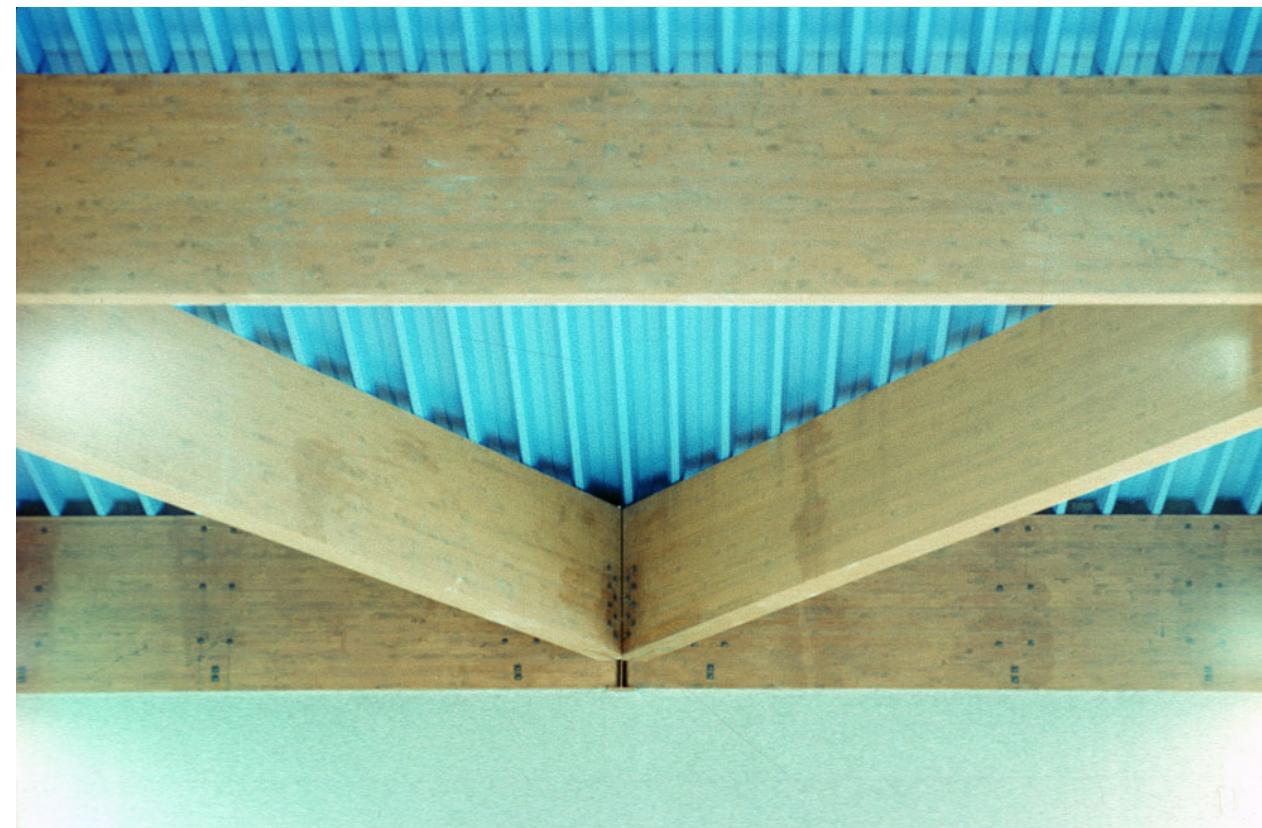








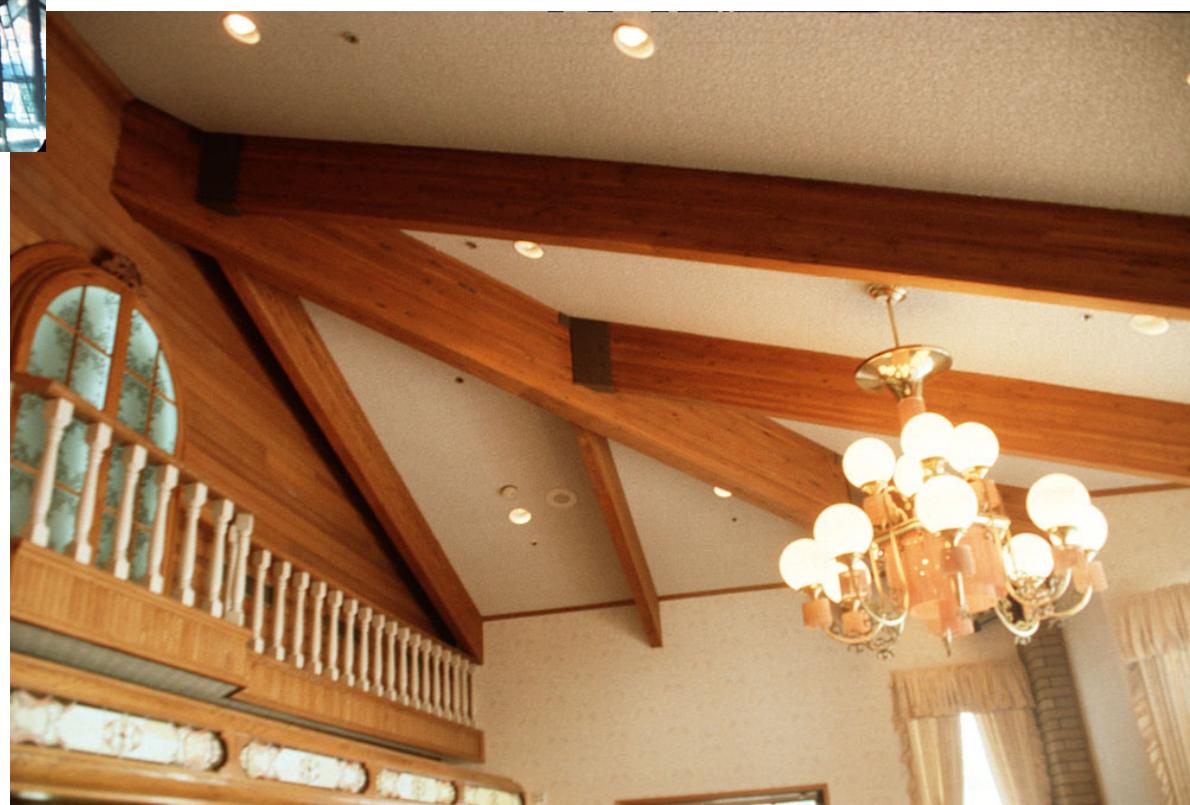
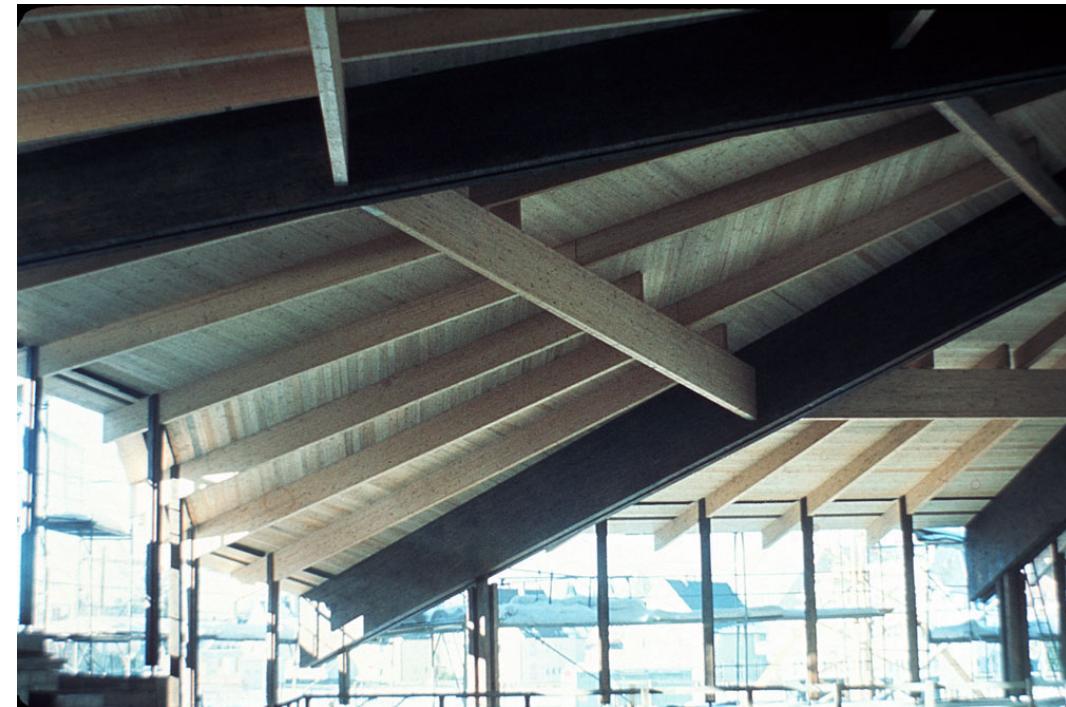






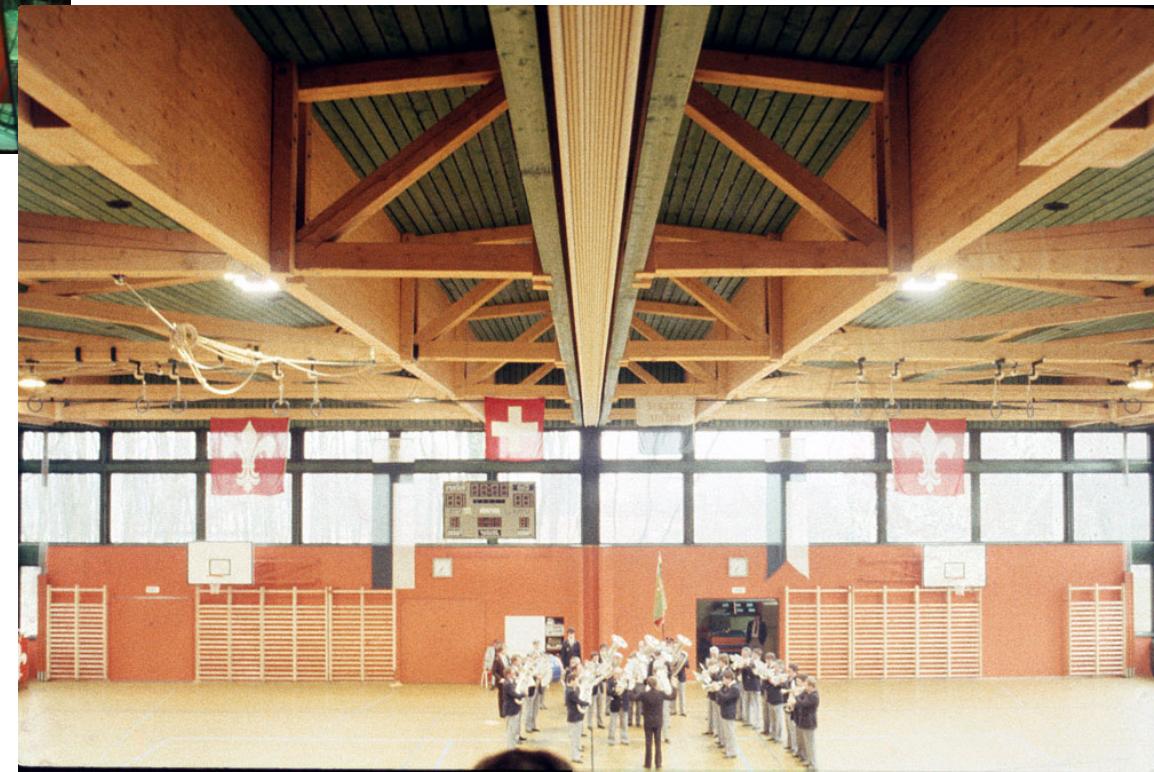








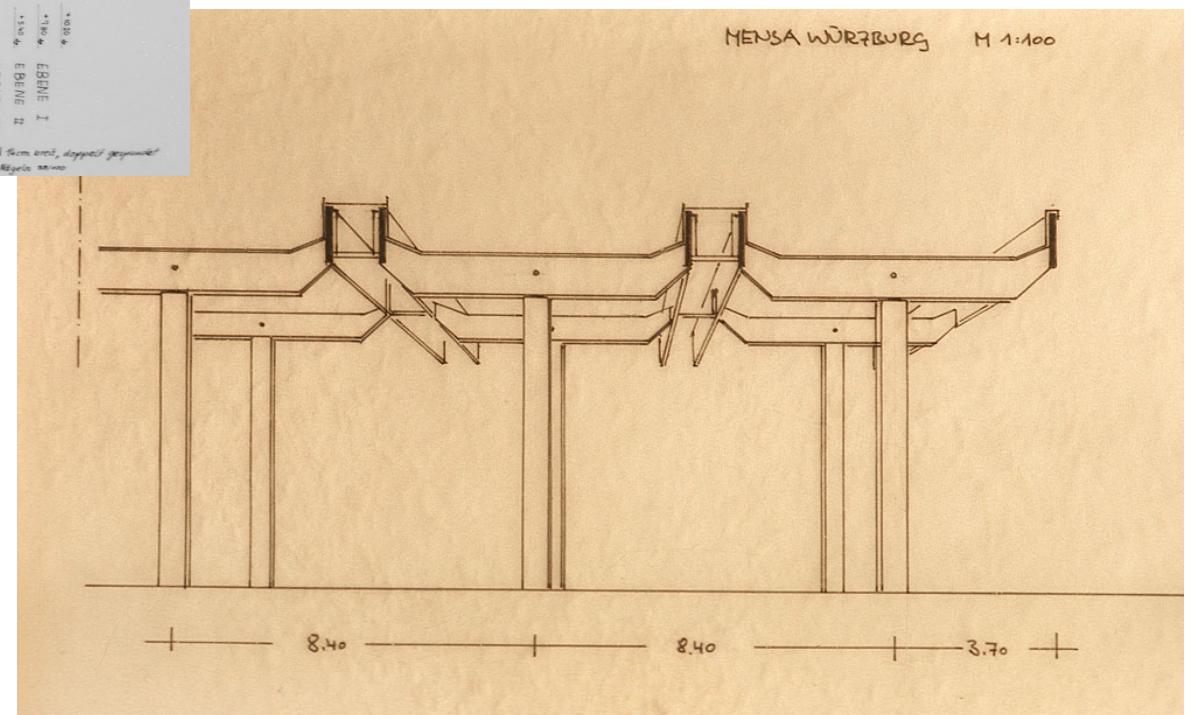
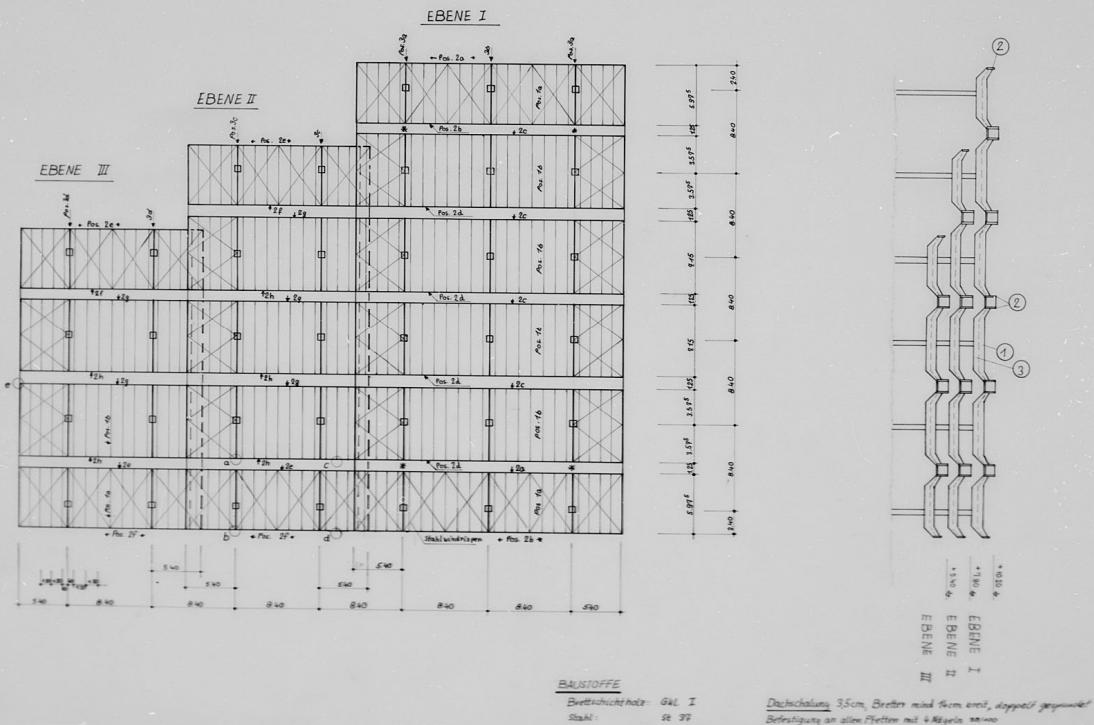




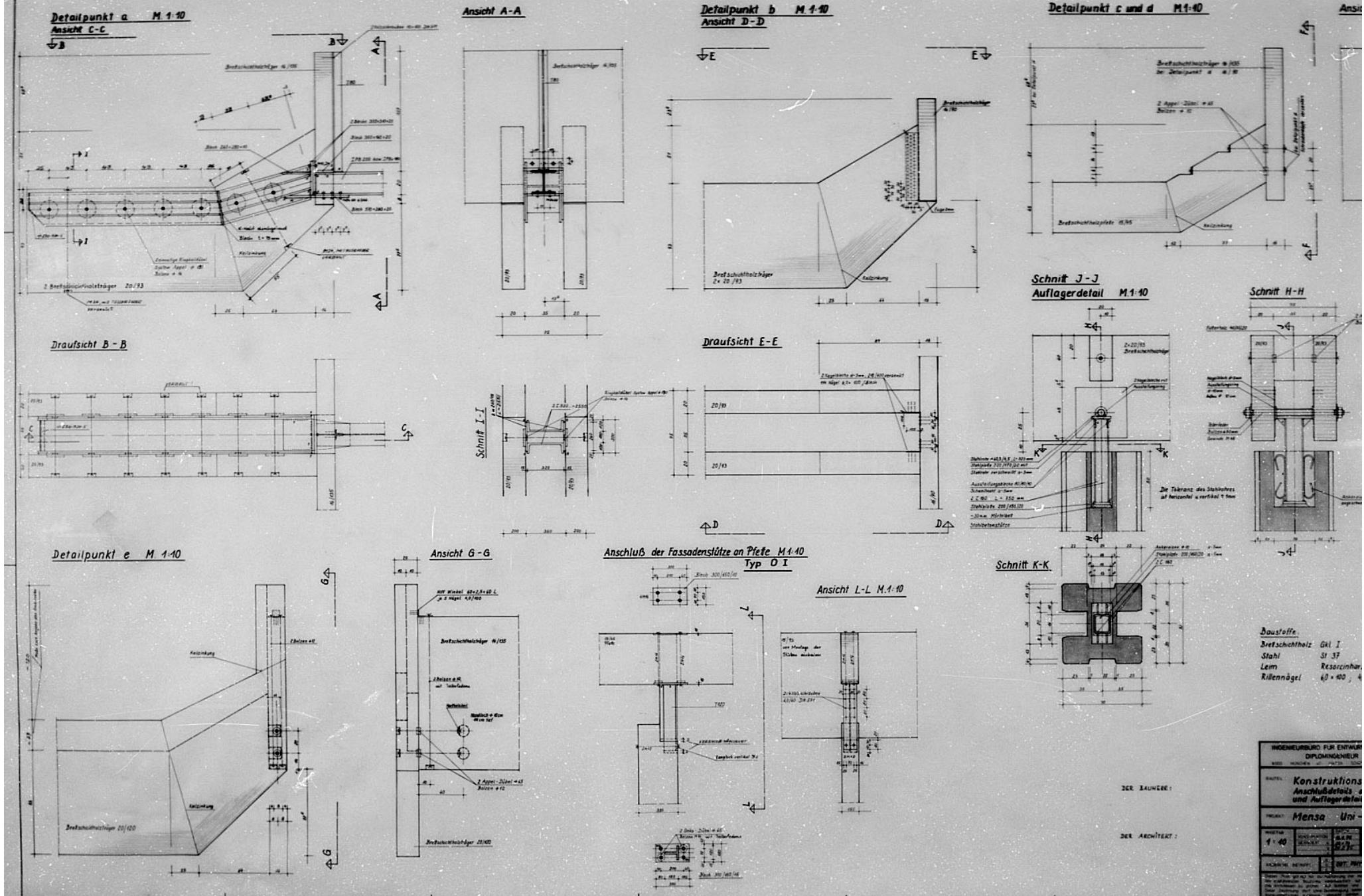


## GRUNDRISS

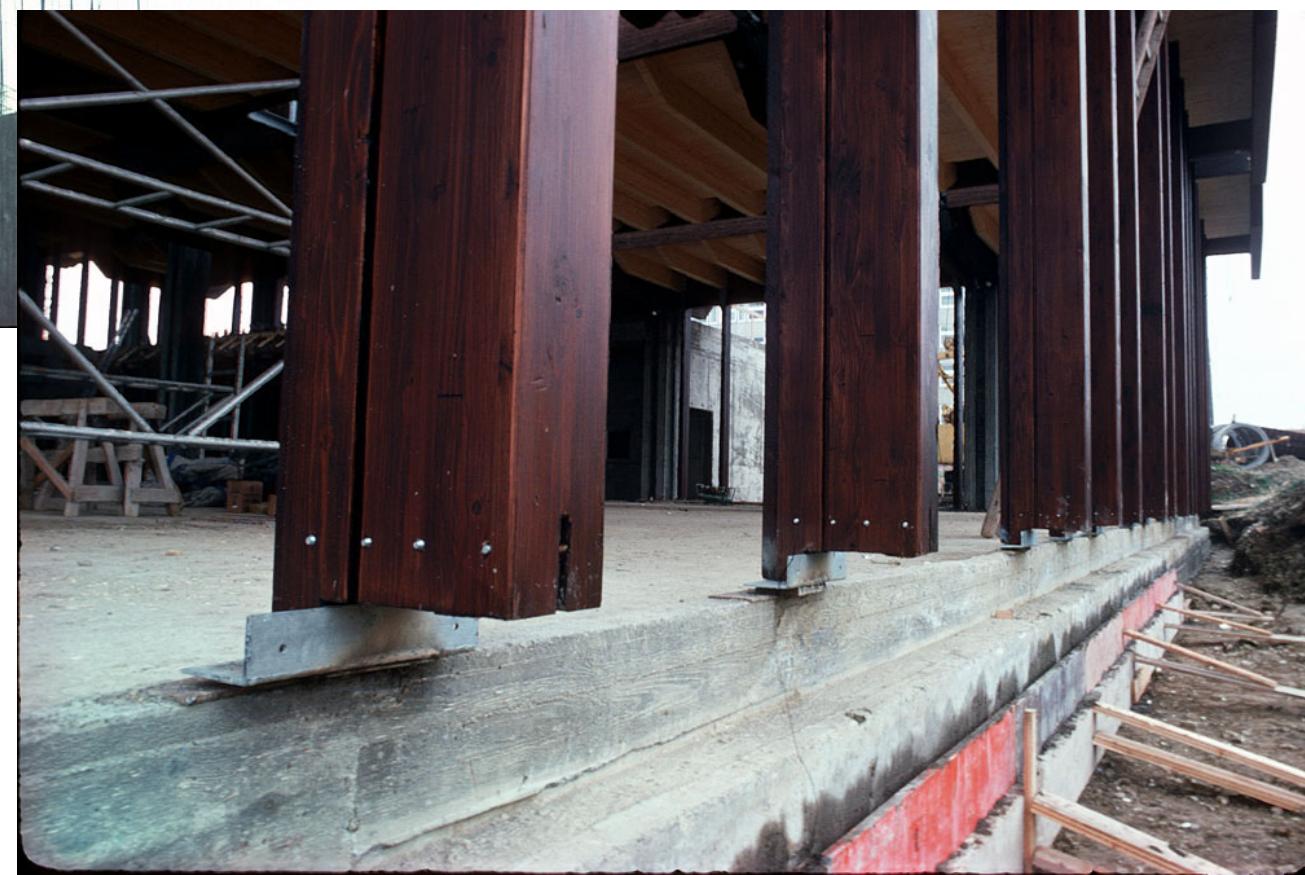
M 1:200



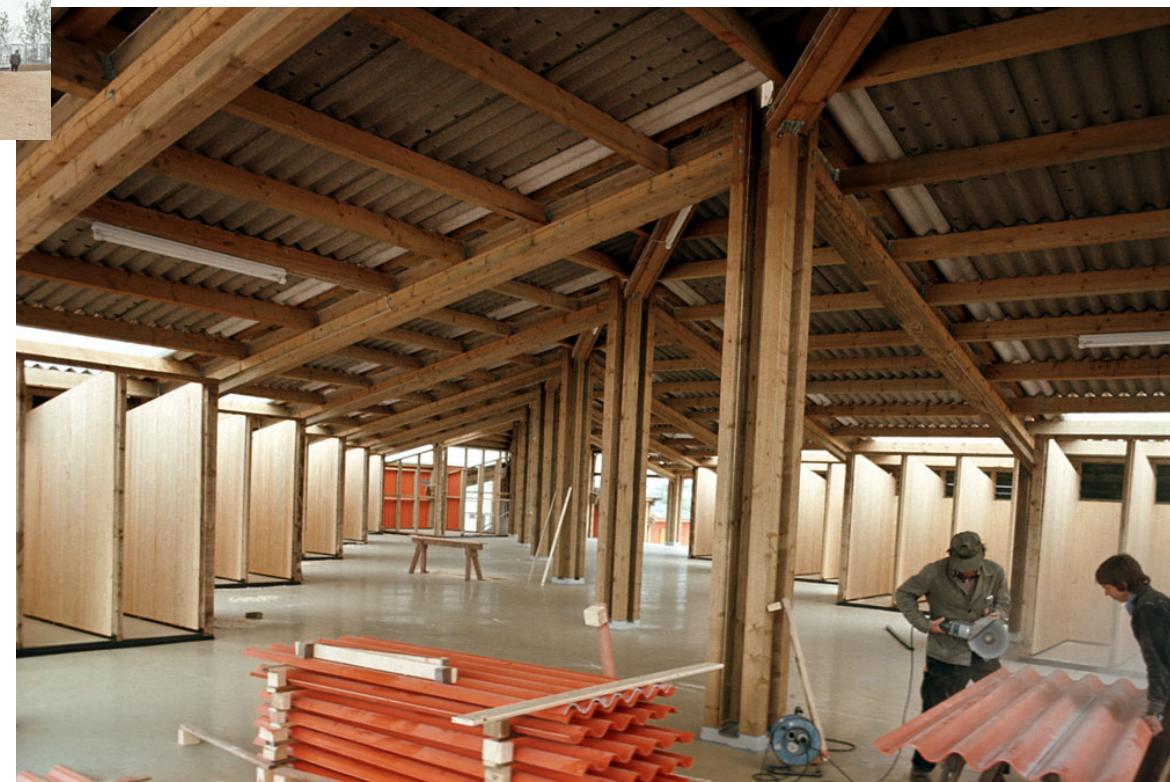










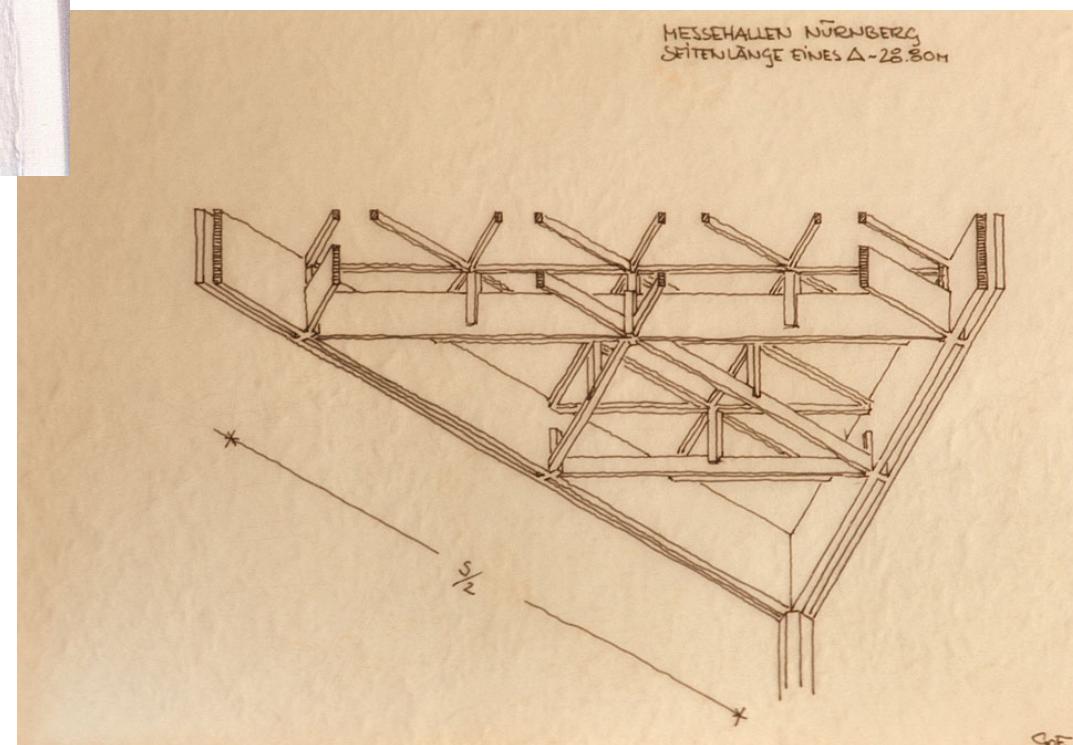
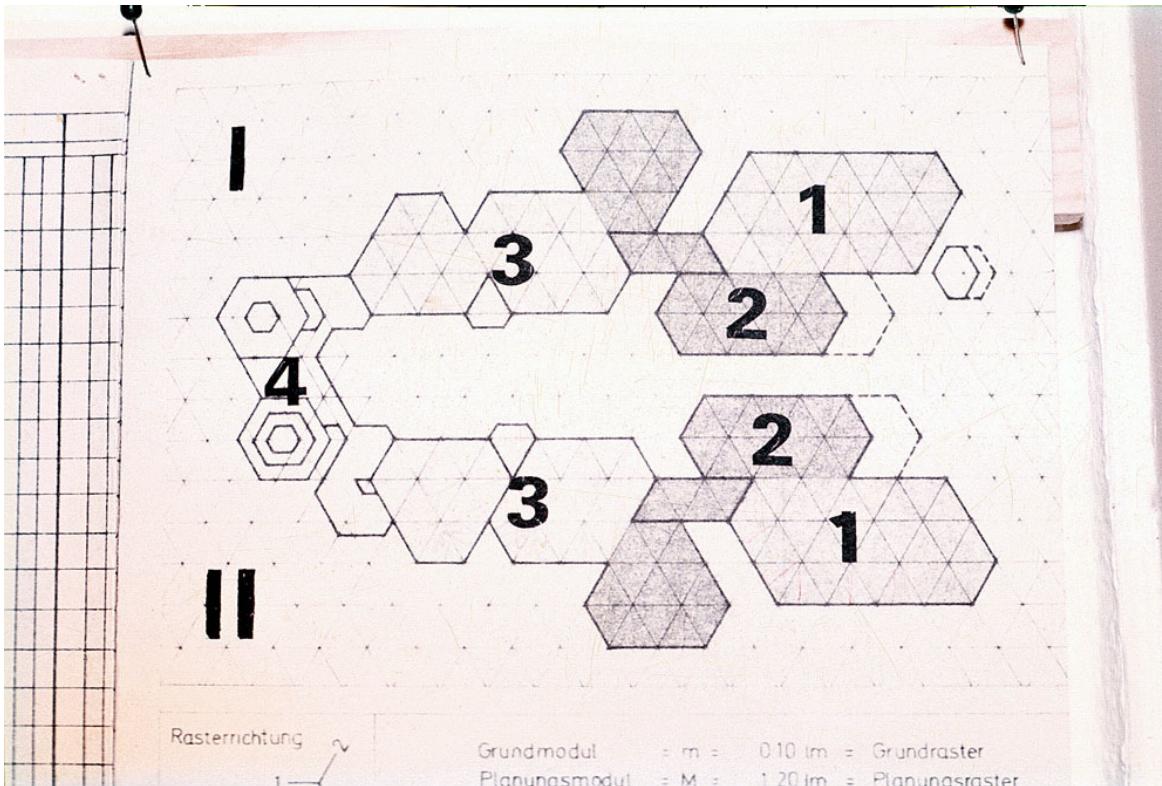


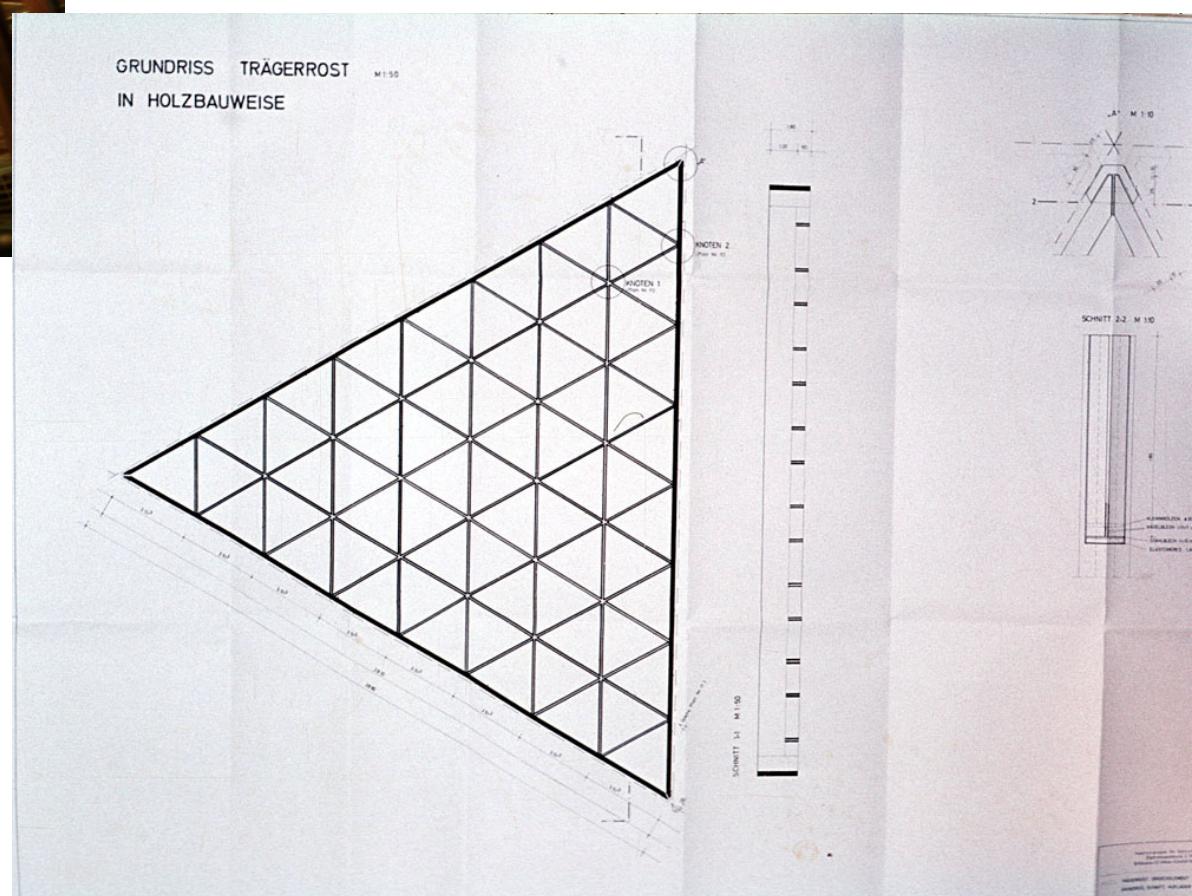


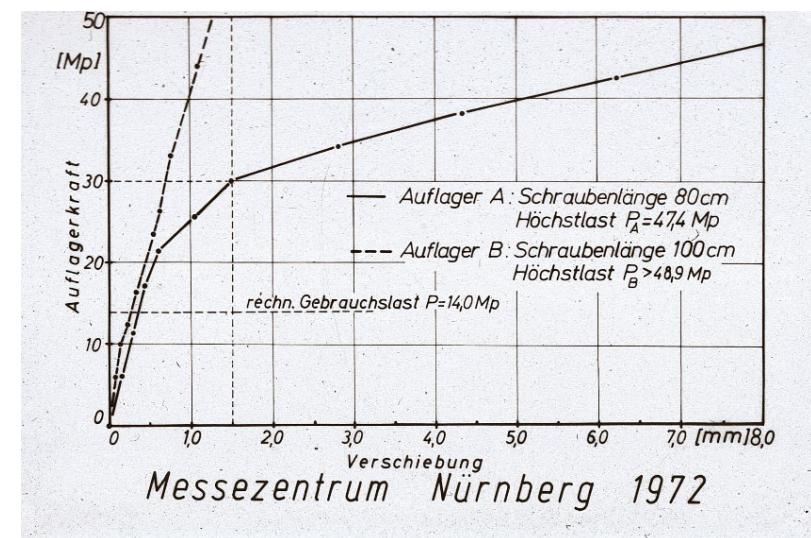
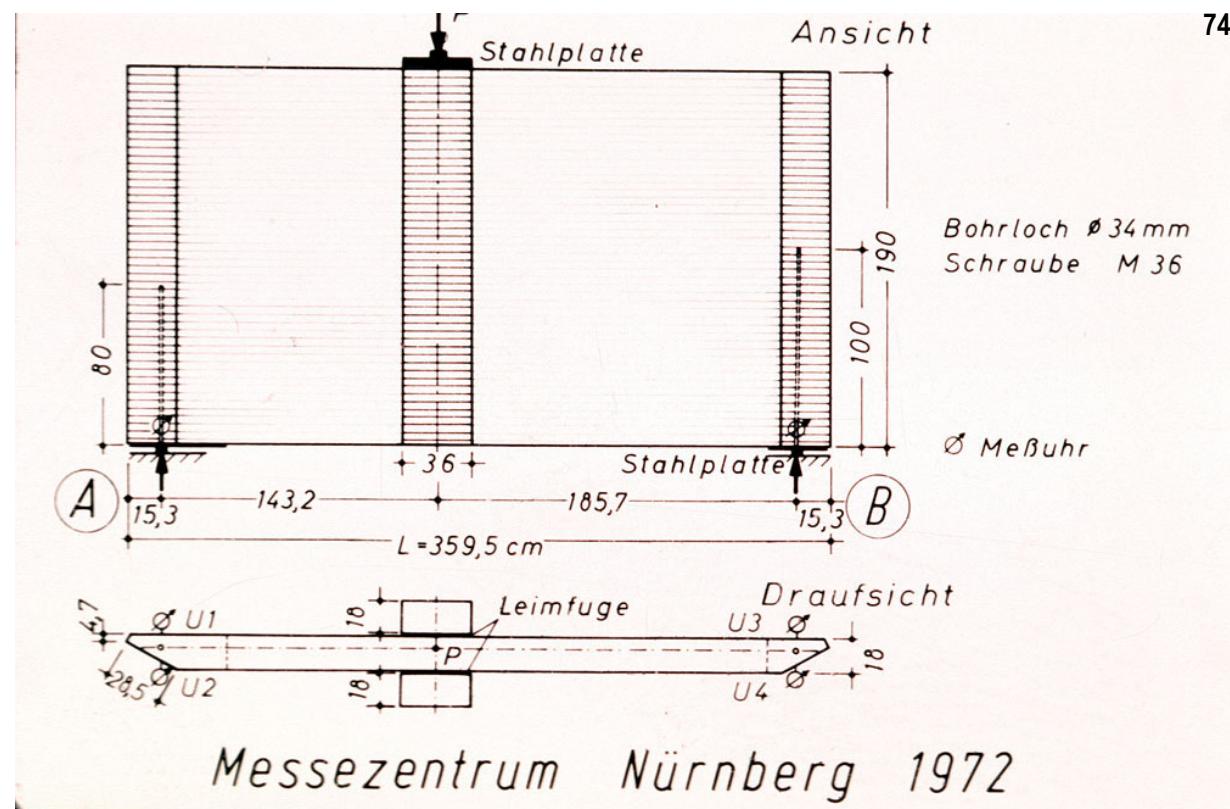
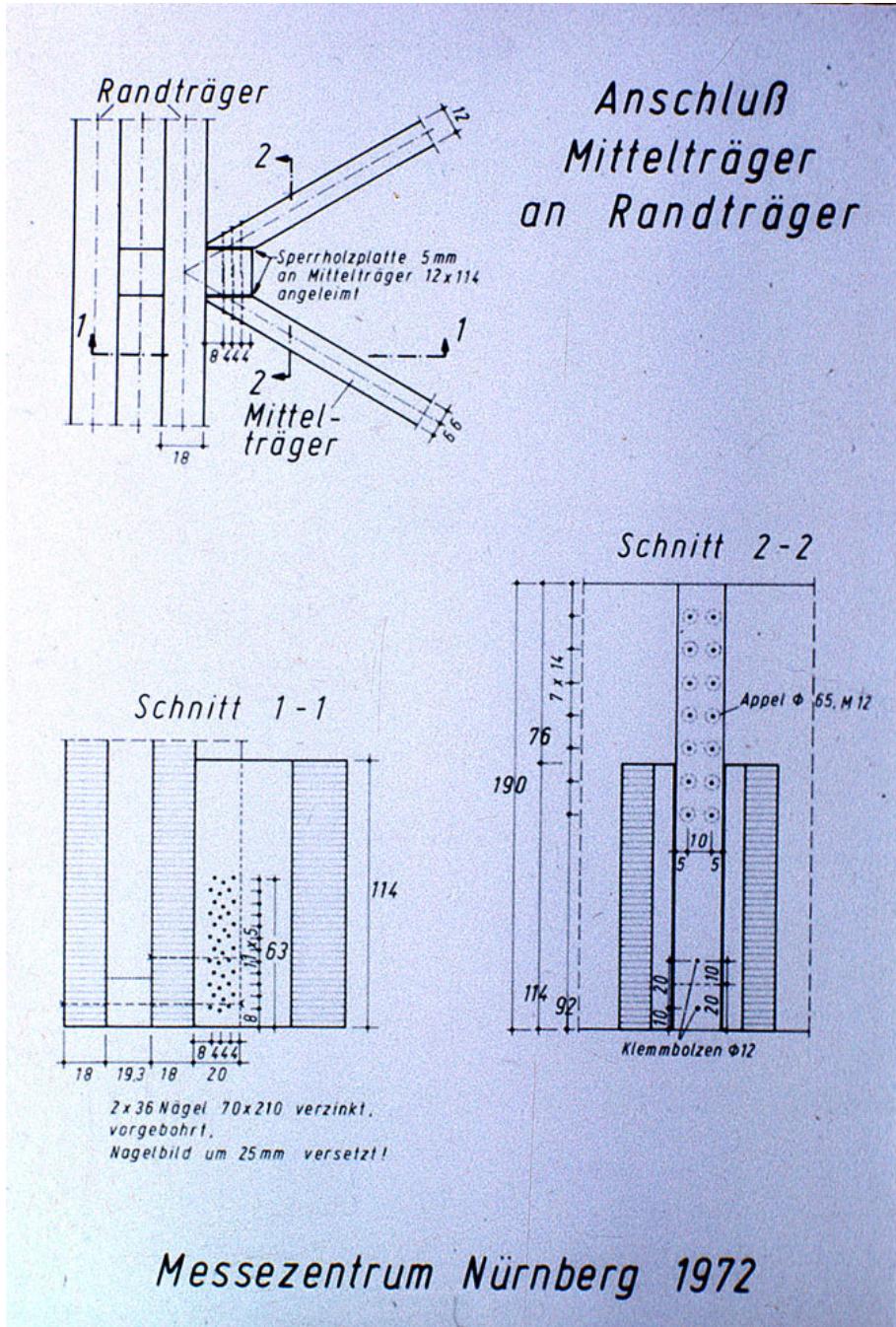


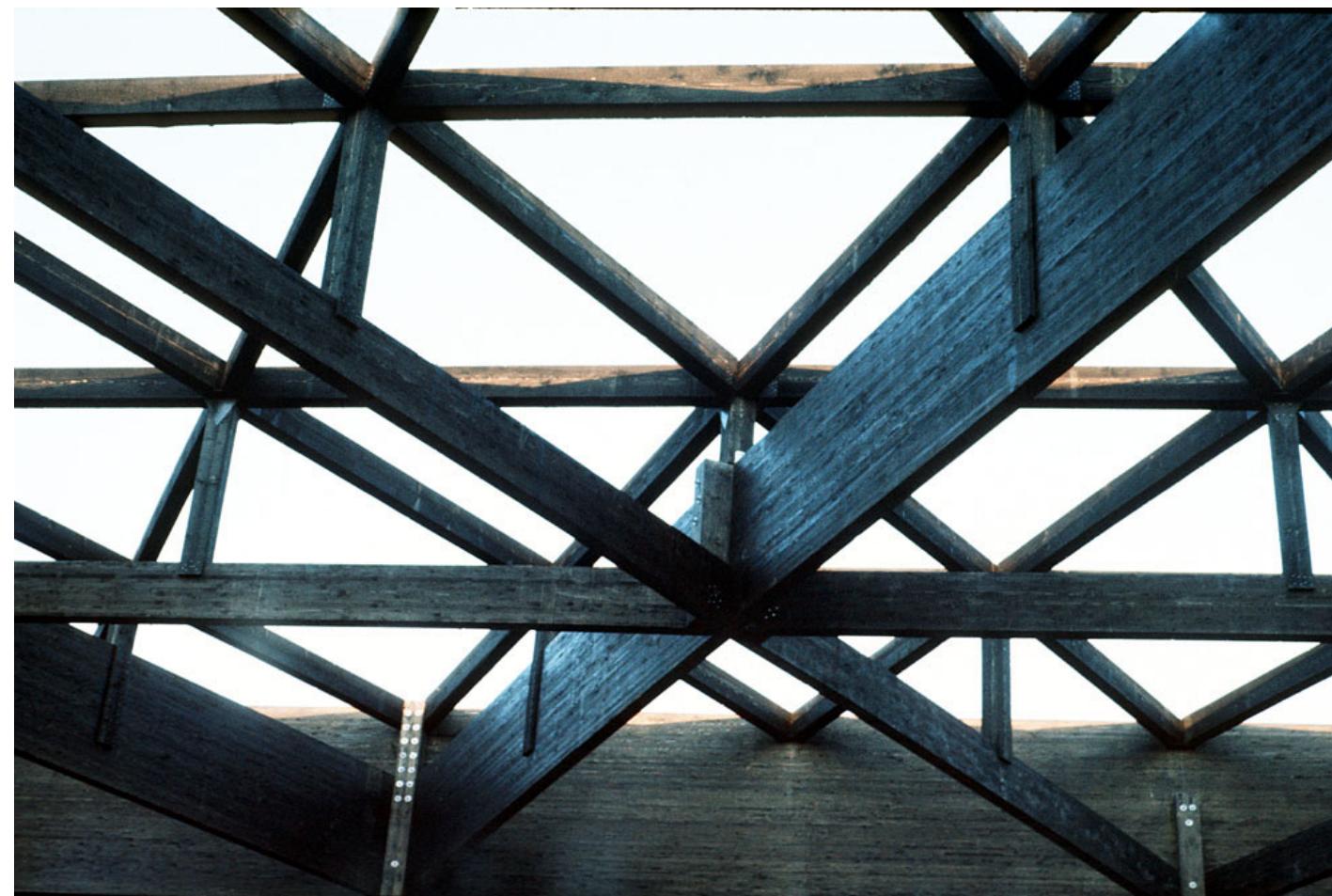






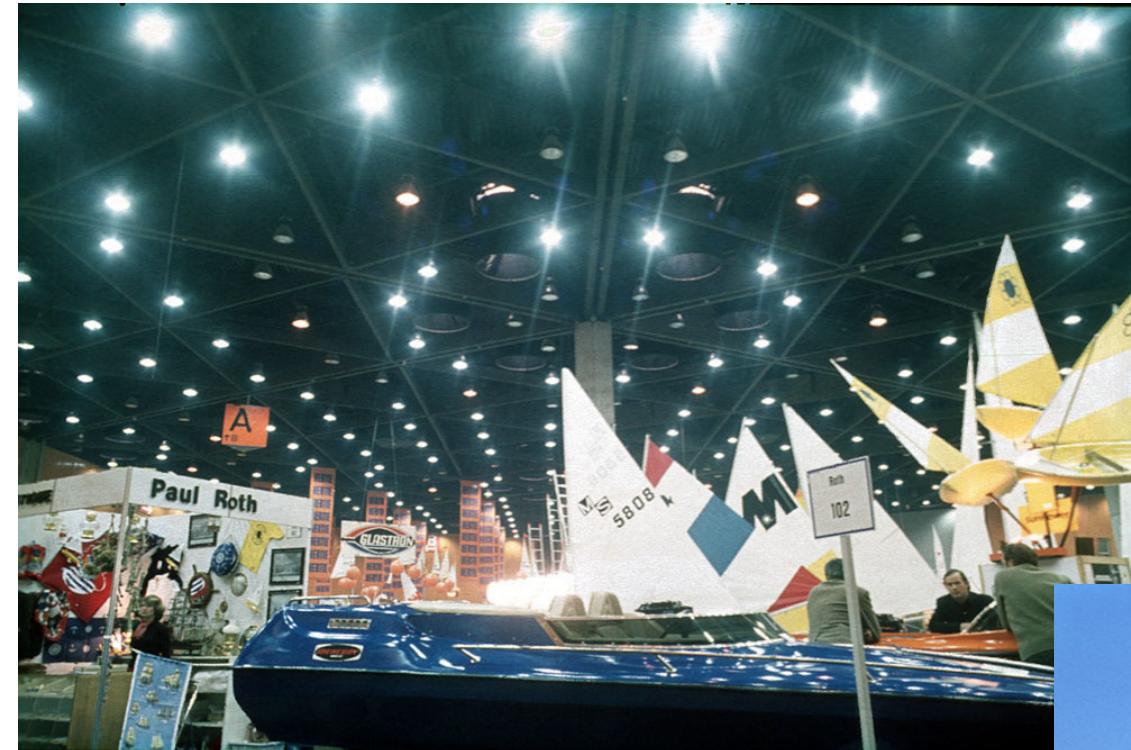






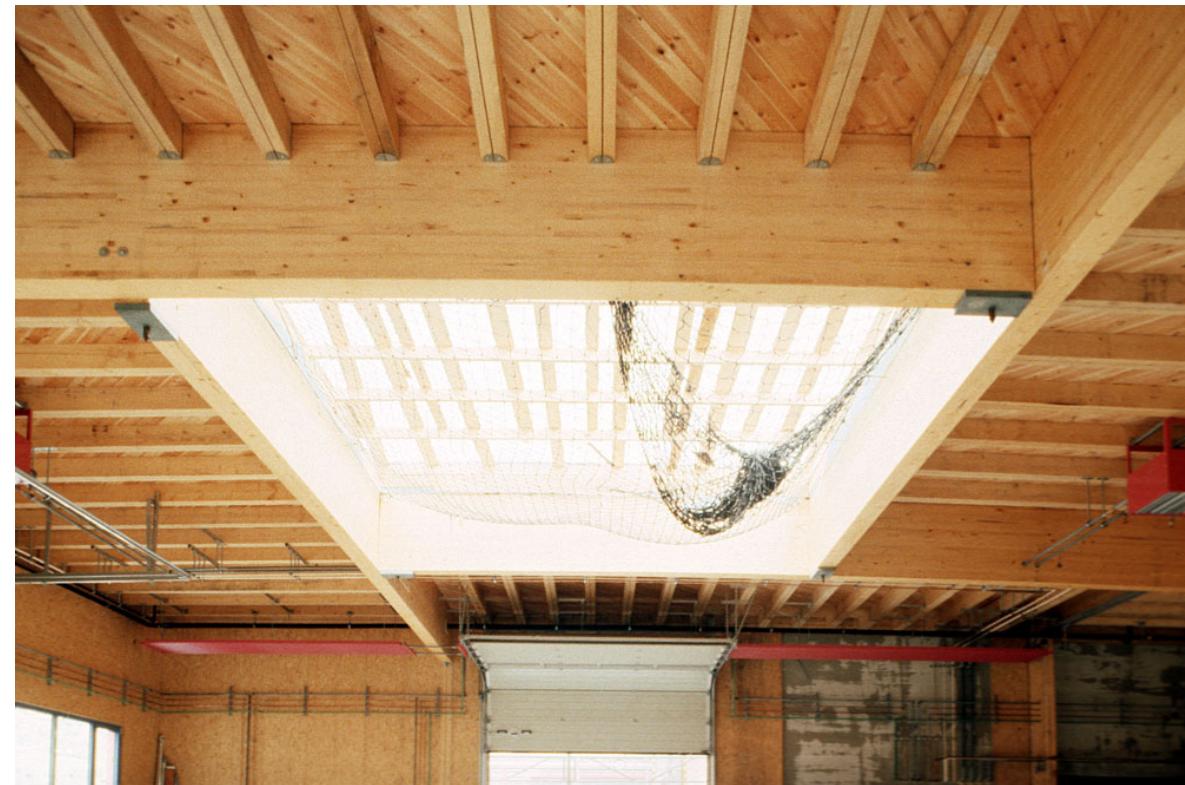




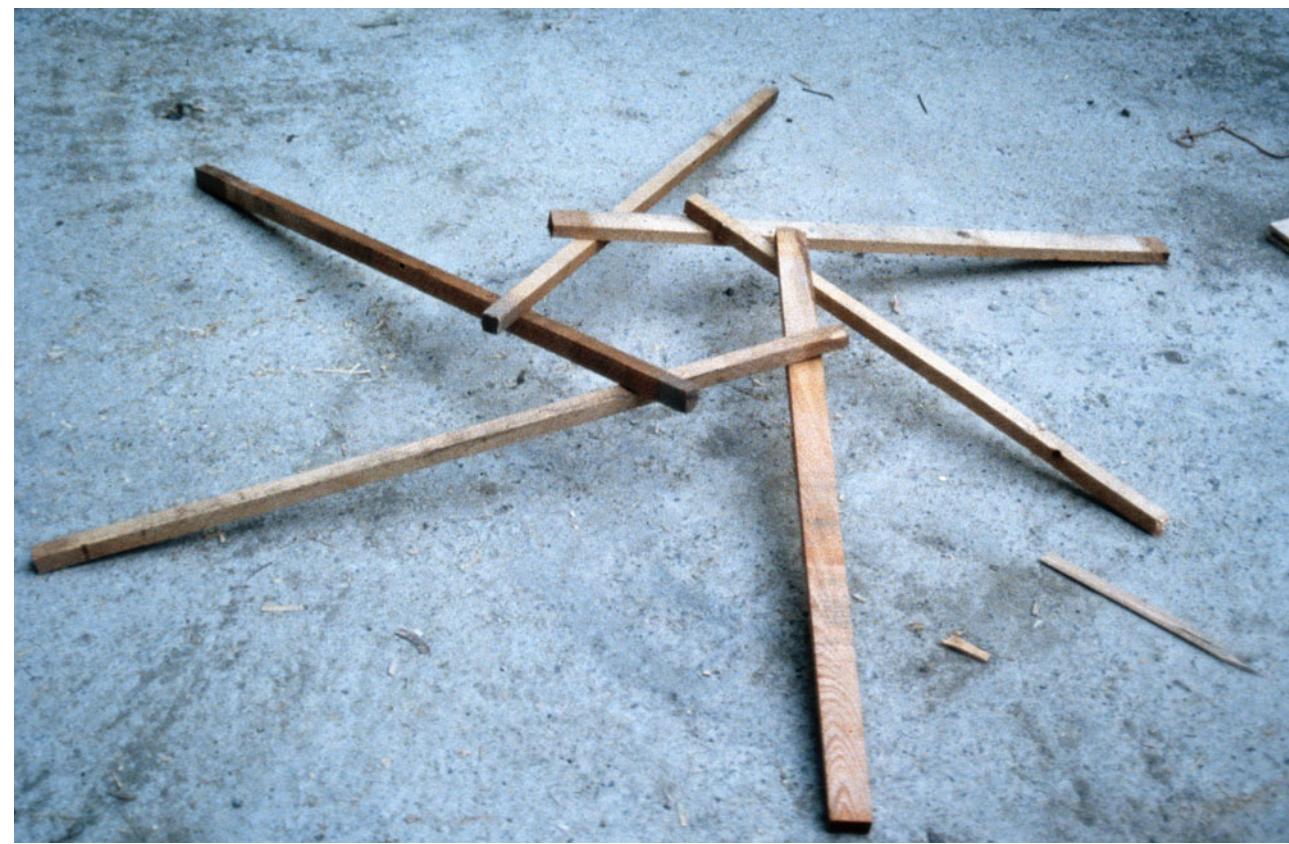




# Reciprocal beam systems



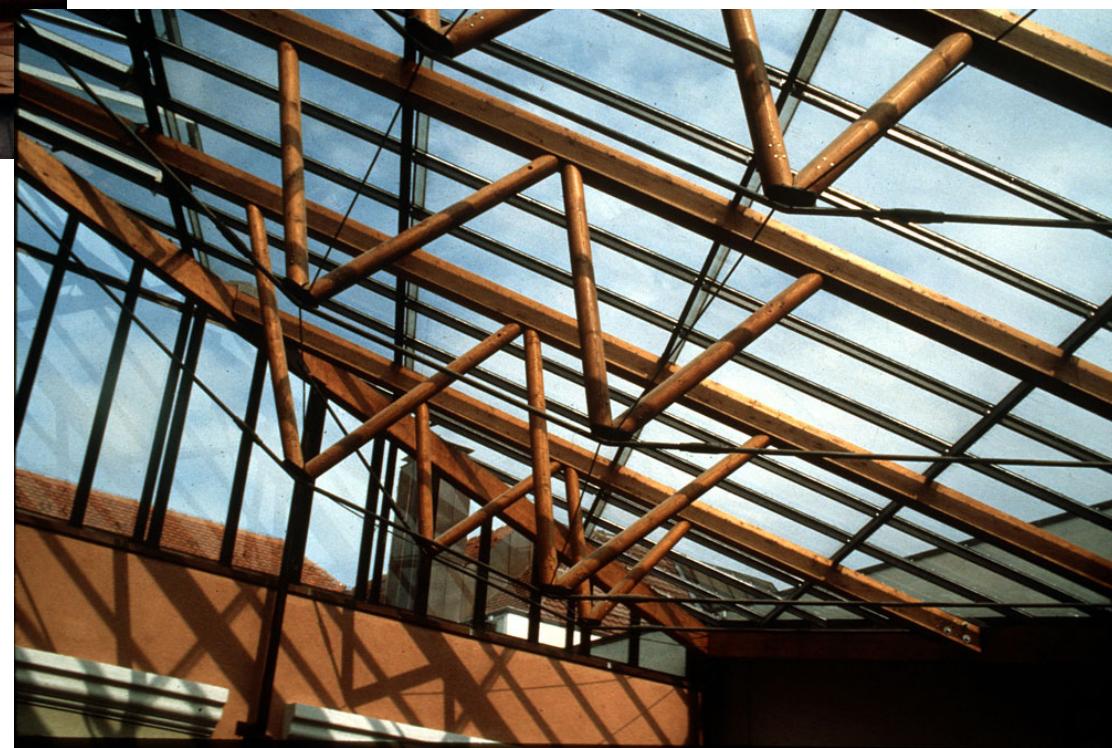




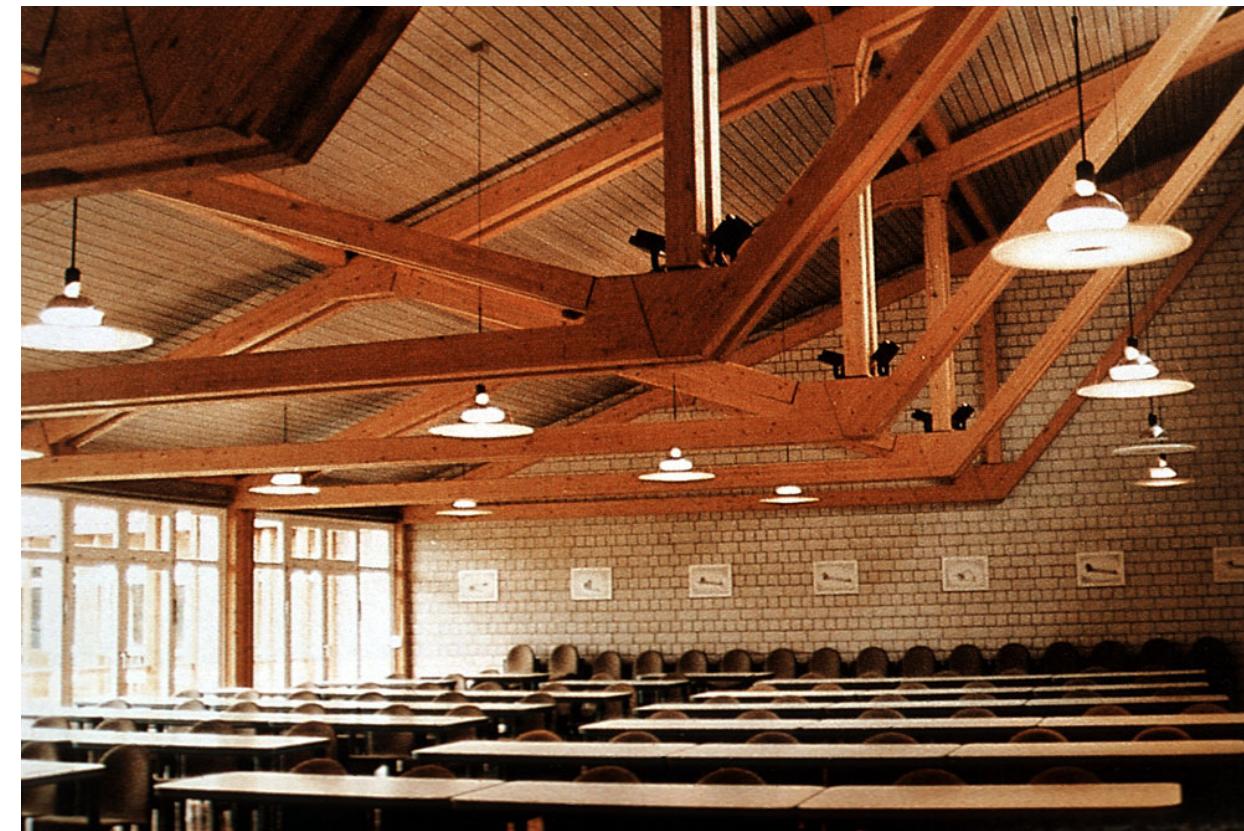




# Poutre sous-tendue



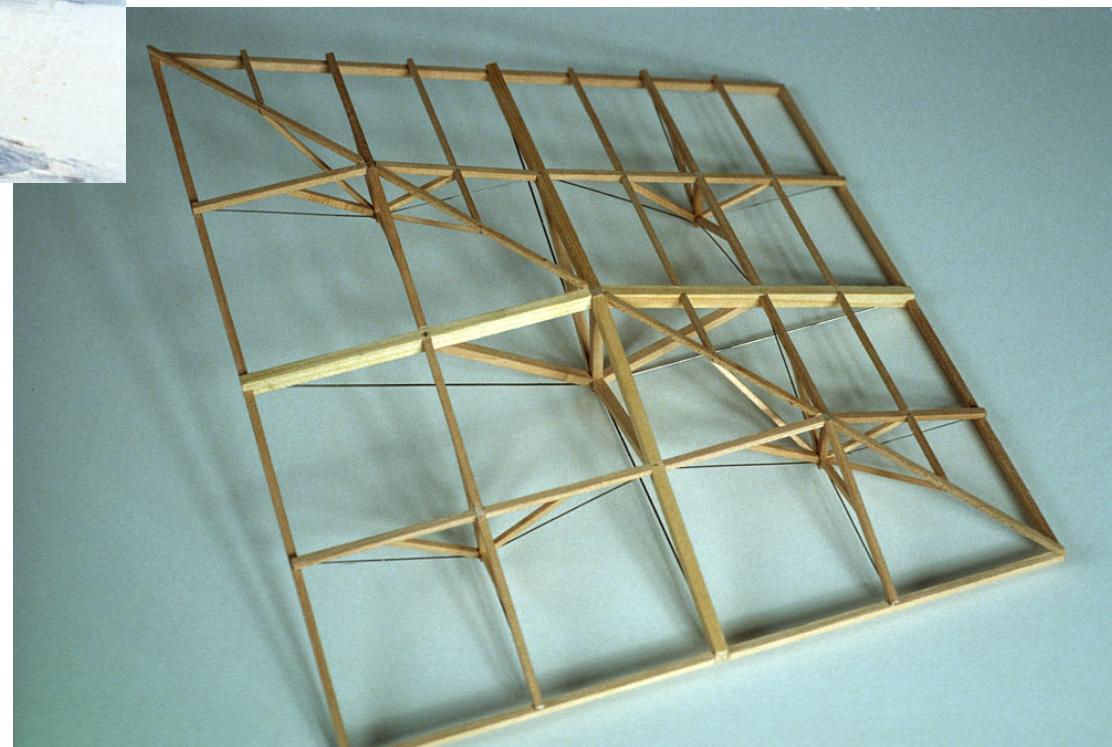










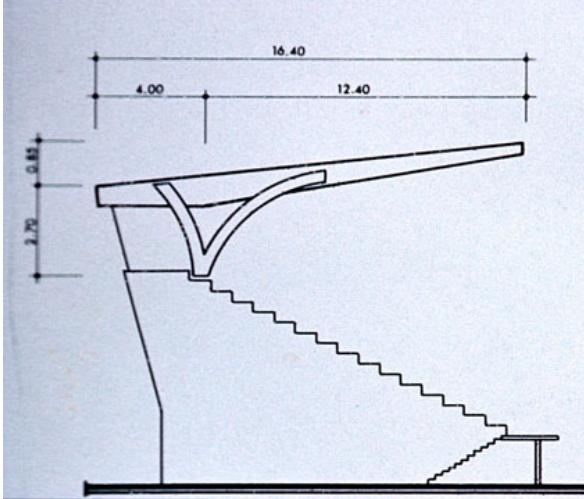


# Système à porte à faux

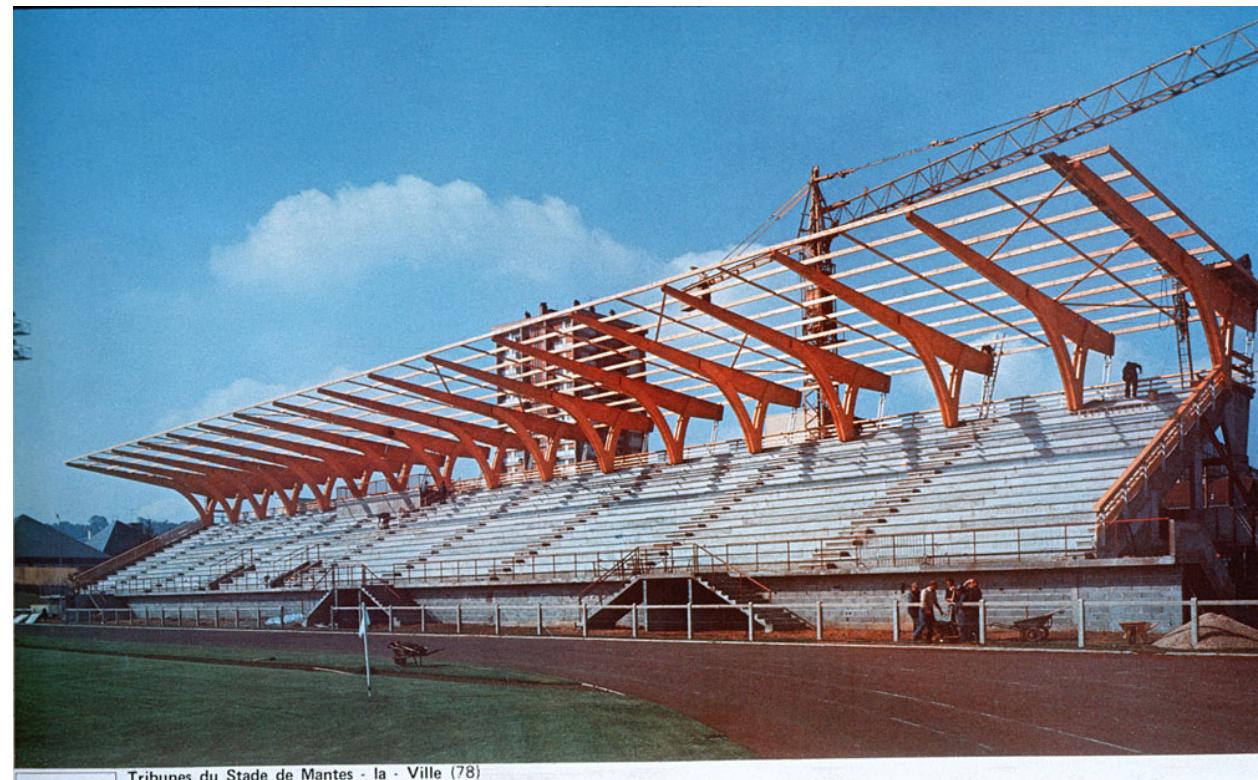








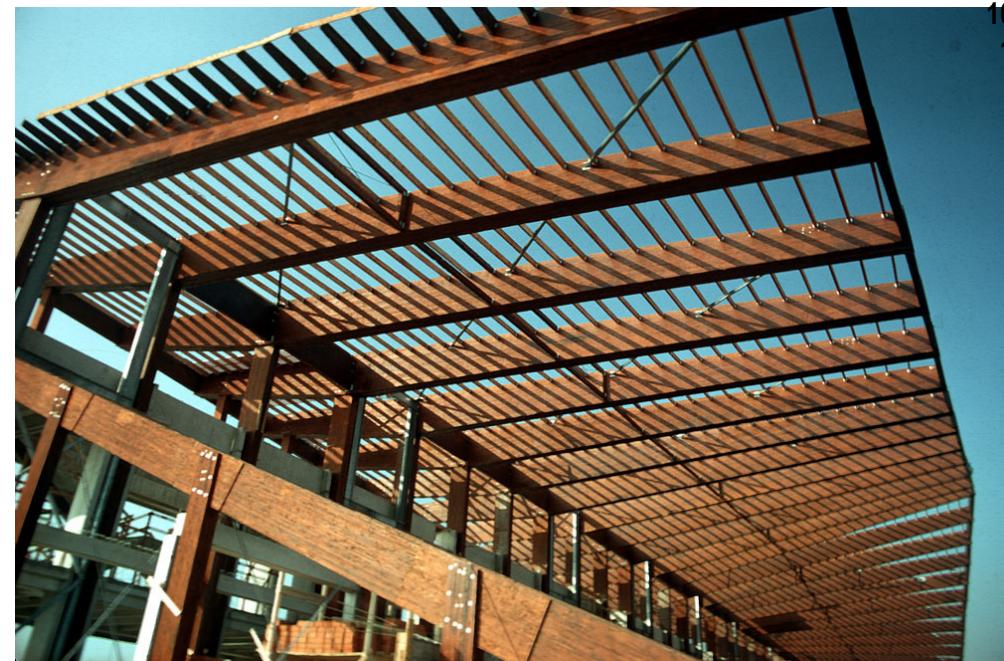
*OSSATURE : Poutres consoles avec tirants métalliques arrières*  
Longueur totale : 86,40 m en 16 travées de 5,40 m  
Couverture en Balithe A.20



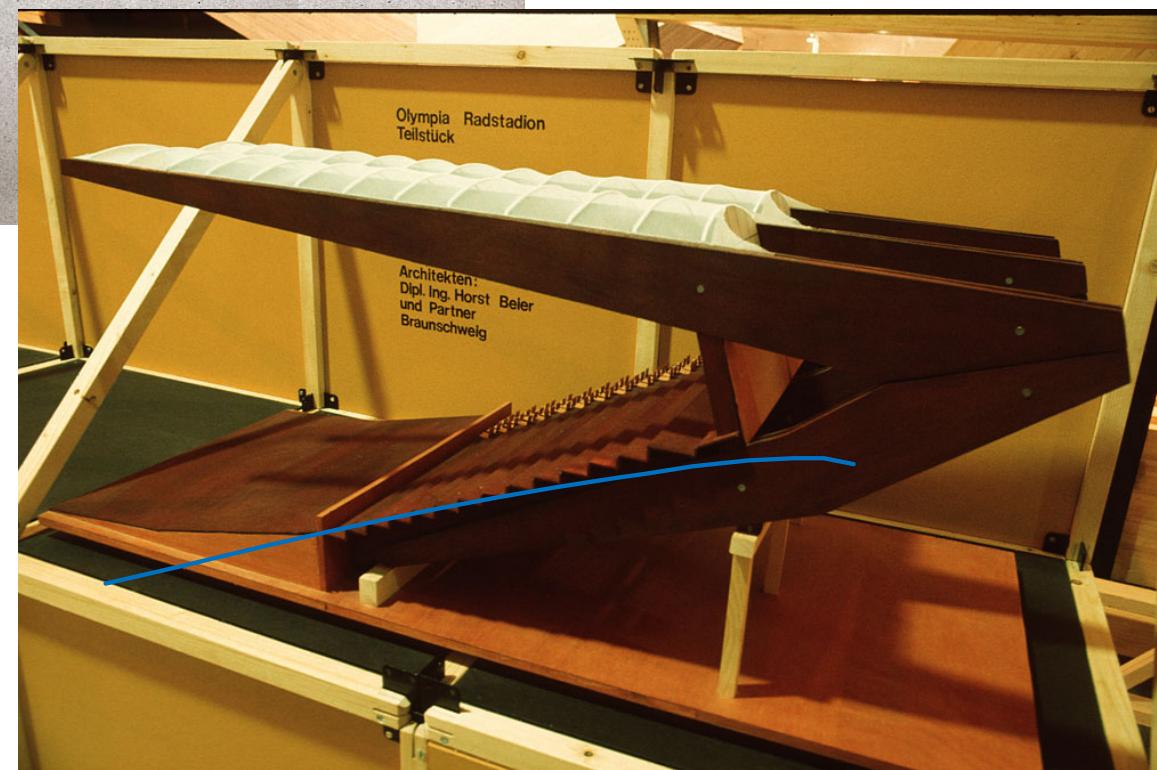
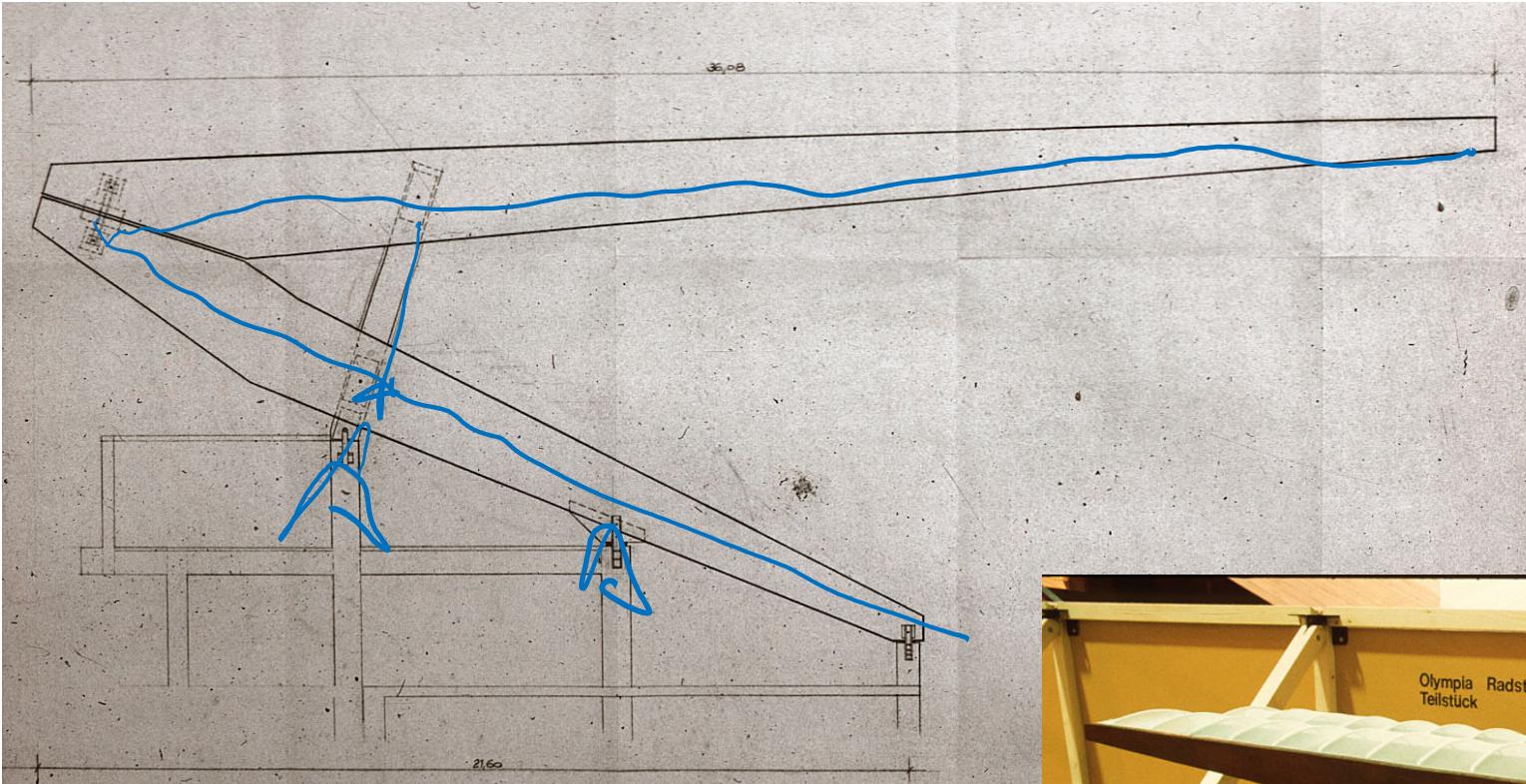
Tribunes du Stade de Mantes - la - Ville (78)

















merci